Seismicity and subsidence following the 2011 Nabro eruption, Eritrea: Insights into the plumbing system of an off-rift volcano

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Abstract

Nabro volcano, situated to the east of the Afar Rift Zone, erupted on 12 June 2011. Eruptions at such off-rift volcanoes are infrequent, and consequently, the plumbing systems are poorly understood. We present posteruption Synthetic Aperture Radar (SAR) images from the TerraSAR-X satellite and post-eruption continuous seismic activity from a local seismic array. Interferometric analysis of SAR data, reveals a circular, 12 km wide, signal subsiding at ~200 mm/yr. We inverted for the best fit Mogi source finding a 4 ± 1 × 107 m3/yr volume decrease at 7 ± 1 km depth. Between 31 August and 7 October 2011, we located 658 and relocated 456 earthquakes with local magnitudes between 0.4 and 4.5. Seismicity beneath the SE edge of Nabro at 11 km depth is likely associated with high strain rates from deep magma flow into the modeled reservoir. This suggests that magma is supplied through a narrow conduit and then stored at ~7 km depth. We interpret seismicity at 4–6 km depth as brittle fracturing above the inferred magma reservoir. Focal mechanisms delineate a thrust fault striking NE-SW and dipping 45° to the SE across the caldera floor. We propose that the crustal response is to slip on this fault which crosscuts the caldera rather than to deform on ring faults. The NE-SW fault plane is not associated with measurable surface deformation, indicating that it does not contribute much to the caldera deformation. We show that subsidence of the caldera is controlled by magma chamber processes rather than fault slip.

1. Introduction

During continental rifting the majority of active volcanism typically becomes focused in a central rift axis [Ebinger and Casey, 2001]. In the Afar region of Ethiopia, this is expressed as laterally stepping en echelon volcanic ranges that accommodate most of the extension [Hayward and Ebinger, 1996]. However, volcanic structures are also commonly found offset from the axis of spreading [Ebinger, 1989; Kiselev, 1987; Abebe et al., 1998; Sturkell et al., 2003; Bosworth et al., 2005]. Termed “off-axis” or “off-rift” volcanoes, their magma supply and their role in accommodating extension remains unclear [e.g., Maccacceri et al., 2014]. Furthermore, eruptions of off-rift volcanoes are infrequent, limiting opportunities to observe them when active. The eruption of Nabro volcano on 12 June 2011 was only the second eruption of an off-rift volcano associated with the Afar Rift Zone (ARZ) in modern times (since Dubbi volcano in 1861 [Wiart and Oppenheimer, 2000]). It was also the volcano’s first in the historical period [Wiart and Oppenheimer, 2005]. Here we analyze post-eruption seismicity and Interferometric Synthetic Aperture Radar (InSAR)-derived surface deformation to understand the subsurface magmatic system of this hazardous, off-rift volcano.

Nabro volcano is located on the central part of the Danakil microplate on the southern margin of the Danakil Alps [Berhe, 1990] in NE Afar (Figure 1). It is the largest volcano in the ~110 km long Nabro Volcanic Range (NVR), which trends NNE-SSW and extends from Bara’ Ale volcano in Ethiopia to the Kod All formation in the Red Sea [Wiart and Oppenheimer, 2005]. A subsection of the NVR is the Bidu Volcanic Complex (BVC) composed of the Nabro and Mallahle calderas. Nabro comprises a horseshoe-shaped caldera reaching 8 km in diameter, open to the SW and facing the smaller 6 km diameter caldera of Mallahle volcano [Wiart and Oppenheimer, 2005]. The summit of Nabro is 2248 m above sea level (asl), making the BVC one of the largest massifs in the Afar region.
Between 23 February and 11 June 2011, nine earthquakes with local magnitudes ranging from 2.6 to 4.8 occurred in the BVC region [Goitom et al., 2014]. These were the first signs of forthcoming volcanic activity at Nabro in modern times. The eruption began between 20:30 and 20:45 UTC on 12 June 2011 from a circular vent region, centered on 41.7°E, 13.4°N and lasted approximately 2 weeks. Explosive phases of the eruption generated ash clouds which reached initial heights of 15–17 km [Clarisse et al., 2014] and disrupted aviation [Bojanowski, 2011].

In addition, an estimated 4.3 Tg of SO₂ were emitted to the atmosphere during the eruption [Theys et al., 2013]. This was the largest emission of SO₂ by an African volcano following the release of ~4.11 Tg SO₂ during the 1981–1982 eruption of Nyamulagira [Bluth and Carn, 2008]. The 2011 Nabro eruption was one of the most substantial volcanic SO₂ emissions since the 1991 eruption of Mount Pinatubo, which emitted ~20 Tg SO₂ to the atmosphere [Bluth et al., 1992].

A small crater just to the SW of the center of the caldera was the focus of the eruption. By 18 June 2011 this crater infilled with a tephra cone and a 2 km discontinuous alignment of small pits striking NW-SE opened up (Oppenheimerpersonn.com). A 17.5 km trachybasalt to trachybasaltic andesite lava flow travelled for ~4 km SW from the vent region, before turning to the NW (Figure 1). In some places, such as near its terminus, the width of the lava flow is as much as 2 km. Flow margins reached 5–10 m in thickness, but the thickness of the interior of the flow could not be judged in the field and may be substantially higher in places. The extent of the eruption required the Southern Red Sea Administration (SRSA) to form response teams to coordinate the disaster [Solomon, 2012]. In total, seven people died, three were injured and 12,000 were displaced. The total cost of the eruption was estimated at 3 million USD [Solomon, 2012].

In this paper we present observations of the post-eruption deformation obtained with high spatial resolution InSAR and microseismicity recorded between 31 August 2011 and 7 October 2011 using a local array. We invert the deformation field revealed by InSAR to model the subsurface change in magma source volume and associated geometry. In addition, we present hypocenters and magnitudes of the earthquakes recorded by the local seismic station network and use them in combination with the deformation data to interpret subsurface magma plumbing. We calculate fault plane solutions to quantify the style and orientation of fault slip in response to magma withdrawal and to study the evolution of the structure of the caldera after the eruption.
2. InSAR Analysis

2.1. InSAR Data

The TerraSAR-X (TSX) satellite was tasked to acquire “StripMap” SAR images of the region following the eruption on both ascending and descending orbits. The TSX satellite uses an active X band SAR antenna with a wavelength of 31 mm, the incidence angle of the beam varies across the scene, between 25.1° to 30.5° and 31.7° to 34.8° for the ascending and descending tracks, respectively. Each fringe within an interferogram corresponds to a change in range of ∼15 mm between the ground and the satellite. Each SAR scene is 30 km wide and 50 km long, large enough to cover the BVC and the surrounding area, with a minimum pixel size corresponding to 3 m on the ground. We used a data set of 25 images acquired between 1 July 2011 to 5 October 2012 on descending orbit 046 and complemented these with 19 images from ascending orbit 130 spanning the period between 6 July 2011 and 10 October 2012.

2.2. Method

The potential for spaceborne radar interferometry to monitor long-term deformation over active volcanoes was first demonstrated by Massonnet et al. [1995]. Subsequently, it has become an invaluable technique to study the ground displacements caused by magma movements due to the high spatial resolution and synoptic coverage of the data [e.g., Amelung et al., 2000; Lu et al., 2005; Wright et al., 2006; Biggs et al., 2011; Hooper et al., 2012]. We created 34 interferograms from the descending data set and 21 interferograms from the ascending data set. The interferograms have a maximum perpendicular baseline of 200 m and temporal baseline between 11 and 390 days. We used a connected network of interferograms which had at least 90% of the image unwrapped (Figure 2). The interferograms were created using the JPL/Caltech ROI_PAC software [Rosen et al., 2004], and we used the multinterferogram method of Biggs et al. [2007] as implemented in \( \pi \) RATE [Wang et al., 2012] to produce a rate map showing the average Line Of Sight (LOS) displacement rate of each pixel, as well as a time series of this displacement.

2.3. Results

In both ascending and descending data sets, we observe a nearly circular, ∼12 km wide range increase, which is centered on the SW region of Nabro’s caldera (Figure 3). As the signal is a range increase in both data sets, the ground surface is moving away from the satellite. Therefore, the volcano is subsiding following the eruption. The caldera region within the descending rate map is incoherent, so we cannot measure the subsidence close to the vent region. In the descending track, the extent of the 17 km long lava flow emplaced by the eruption is also clearly distinguishable as an incoherent region originating from the caldera. There maybe a small localized loading effect within ∼50 m of the lava flow. The ascending track is more coherent within the caldera; the maximum subsidence rate we measure is ∼200 mm/yr. There is a small amount of LOS ground deformation at Mabda, Mallahle and Sork’Ale volcanoes observable from the ascending rate map (Figure 3); we interpret this as atmospheric noise caused by the topography of the volcanoes, as it is not visible in the descending data set. We have also plotted the subsidence over time (Figure 4) recorded at 1 pixel in the ascending data set. We find that the subsidence over the observation period is altogether quite linear but may have been faster immediately following the eruption. We go on to model the subsidence assuming a linear rate over time.
Figure 3. Best-fit model assuming Mogi and sill sources. (a) Observed ascending rate map of ground movement, white point: pixel used for time series. (b) Mogi model of deformation for ascending track. (c) Residual motion following Mogi model. (d) Sill model of deformation for ascending track. (e) Residual motion following sill model. (f) Observed descending rate map of ground movement. (g) Mogi model of deformation for descending track. (h) Residual ground motion. (i) Sill model of deformation for descending track. (j) Residual ground motion. (k) Profile of ground displacement along transect N-S on Figure 3a. (l) Profile of ground displacement along transect W-E on Figure 3a. The black squares in Figures 3a and 3f show the far-field regions used to calculate noise for the Monte Carlo analysis. The red points in Figures 3b, 3d, 3g, and 3i, mark the center of the model at depth. The interferograms span 462 days for both the ascending and descending tracks.

We jointly inverted the ascending and descending ground displacements using a Monte Carlo hybrid downhill simplex inversion technique [Clarke et al., 1997; Wright et al., 1999], which assumes a homogeneous, isotropic, Poisson-solid half space. The rate maps were averaged to 1 km pixels to reduce the inversion time. We first considered a deflating Mogi source in an elastic half space and solved for the depth, location, and volume change of the source (Figure 3). Uncertainties on these parameters were calculated using a Monte Carlo hybrid downhill simplex inversion technique.
Carlo simulation by adding correlated noise to the data set [Wright et al., 2003], which was estimated from a background reference region located away from the deformation (Figure 3). We created 100 of such data sets, which were subsequently inverted. The range of the solutions gives the uncertainties of the parameters. We find the best-fitting Mogi source at 7 ± 1 km depth, which reduces in volume by 4 ± 1 × 10^7 m^3/yr, on the surface, the center is located within 0.6 km of 13.35°N and 41.69°E. From the Monte Carlo simulations we find a trade-off between the volume change and the depth of the source. The ground displacement modeled by the Mogi source has an RMS misfit of 13.2 mm/yr and 11 mm/yr for the ascending and descending tracks, respectively. The highest residuals in the ascending track are around the caldera rim, and highest in the descending track between Nabro and Mallahle calderas. This could be due to the loss of coherence in these areas due to the topography and ash cover or due to the model simplifications.

We also considered a sill geometry to model the subsidence. We used the same Monte Carlo hybrid downhill simplex inversion technique, and in the initial inversions, we solved for the location, depth, size (horizontal extent), and closing of a single-square Okada source [Okada, 1985]. However, the inversion collapsed to a small source with an unphysically large opening. Effectively, the only constraint on the size of the sill is that the horizontal extent of the sill is much less than the depth of the source. We therefore fix the horizontal extent of the sill to be 1 km in the subsequent inversions and only solve for the amount of closing. This is equivalent to solving for the contraction volume of a point source sill. We find that the best-fit sill is located at a depth of 11 ± 2 km; it has a contraction volume of 4 ± 1.2 × 10^7 m^3/yr, and on the surface, the center is located within 0.9 km of 13.35°N and within 0.6 km 41.69°E. As observed with the Mogi source, due to the nonuniqueness of InSAR modeling, there is still a trade-off between volume change and depth. The sill model underestimates the amount of subsidence at the center of Nabro’s caldera, observable from the ascending track. Also, the sill solution does not account for much horizontal movement. This has resulted in higher residuals on the east and west flanks of Nabro in the ascending and descending tracks, respectively. The RMS misfit for the sill model is 13.9 mm/yr and 12.7 mm/yr for the ascending and descending tracks, respectively.

The Mogi model better describes the horizontal ground motions which are implied by the difference between the ascending and descending scenes, suggesting that the surface deformation is best approximated by a deflating point source. The model also captures the maximum surface displacement better than the sill source. Also, the RMS misfit is lower in both tracks and this is emphasized in the transects across the ascending data (Figures 3k and 3l). We have neglected the variation of topography for the inversion, and therefore, we have referenced all depths to 700 m asl, (the seismicity reference elevation). The interferometric analysis and modeling describes the ground displacement and gives an analytical solution to the magma chamber geometry. Using the seismic data we can improve the constraints on the depth of the magma chamber and observe the small scale brittle response to the eruption. These features will further delineate the magma plumbing system and may illuminate faults which accommodate the subsidence. We present the seismic data in the following section and provide a discussion of the integrated results.

### 3. Seismic Analysis

#### 3.1. Seismic Data

In response to the eruption, we deployed a network of eight broadband Guralp seismic stations (five 6TD and three 40TD, provided by SEIS-UK [Brissbourne, 2012]) on the flanks of Nabro. The network was fully operational by 31 August 2011, 79 days after the eruption began. However, the GPS failed at NAB5 (6TD site)...
Figure 5. (top) Initial hypocenter locations determined using Hypo2000, for the 658 earthquakes detected during the period 31 August to 7 October 2011, shown as black dots (map view) and grey dots with error bars (N-S depth profile). The position of 456 relocated hypocenters calculated by HypoDD are shown as colored dots, dependent on their local magnitude. Seismic stations used to locate the events are indicated by black triangles. Yellow outline highlights the vent region. (bottom) Topographic profile and hypocenters along transect A-A’, determined by HypoDD within 1 km either side of the transect. The depths are given referenced to 700 m asl, the lowest elevation seismometer. The histogram shows numbers of hypocenters at depth per 1 km bin. Numbers indicate clusters as described in text.

3.2. Methods

We manually picked arrival times of the P and S waves at every seismic station for each distinguishable earthquake using SAC software [Goldstein and Snoke, 2005]. We found that the traces did not need to be filtered before analysis due to the high data quality. As part of the process, we assigned a quality value of 0, 1, 2, and 3 to the measurement, based on an estimated P wave arrival time error of 0.05, 0.1, 0.015, and 0.2 s, respectively. For S waves, the 0 to 3 quality values were assigned to values of 0.1, 0.175, 0.25, and 0.3 s, for the estimated error in arrival time. These values were used as weights in the location inversion performed by the Hypo2000 algorithm [Klein, 2002] (Figure 5).

During the 38 day recording period we detected a total of 658 earthquakes on Nabro caldera and in the surrounding area. To locate earthquakes we used a 1-D velocity model with a linear increase in velocity with depth [Lahr, 1989]. This avoided clustering of earthquakes at velocity discontinuities, an artefact often observed in velocity models with homogeneous layers. Our velocity model was constrained using crustal scale reflection and refraction seismology across the Danakil blocks [Makris and Ginzburg, 1987]. The average location error using this technique is significant: ± 2 km horizontal, ± 4 km depth, and obscures detailed observations about the magmatic plumbing of the volcano [Jones and Stewart, 1997]. These errors result from a combination of factors including, station locations, available phases, accuracy of the arrival time measurement, and the validity of the velocity model [Waldhauser and Ellsworth, 2000].
Figure 6. For all 658 events. (top) Distribution of the number of earthquakes at each magnitude. Black shows the distribution for all hypocenters, red shows the distribution for those which occurred on Mallahle caldera. (middle) Gutenberg-Richter distributions of the relocated earthquakes on Nabro. (bottom) Gutenberg-Richter distributions of the relocated earthquakes on Mallahle.

The Hypo2000 algorithm locates hypocenters assuming a 1-D subsurface. However, the velocity of a seismic wave beneath an active volcano will vary in three dimensions due to variations in rock composition and partially molten bodies. In addition, the subsurface velocity structure may also change through time as partial melt bodies evolve. We minimized the dependence of the hypocenter location on the velocity model by proceeding with a double differencing technique, HypoDD [Waldhauser and Ellsworth, 2000; Waldhauser, 2001], which we applied to the located events determined by Hypo2000, (Figure 5). We parameterized the relocation procedure in order to relocate the maximum number of events while minimizing the allowed separation between the initial hypocenters. In this manner, 456 of the initial 658 earthquakes were relocated.

Local magnitudes ($M_L$), as originally defined by Richter [1935], were computed using the maximum body wave amplitude of the horizontal components on Nabro. The computation also considers the distance between the earthquake and stations in a distance correction term, which allows for decrease in amplitude with distance due to attenuation. We use the correction term derived for the Main Ethiopian Rift (MER) by Keir et al. [2006]. This correction is applicable to the high ground motion attenuation conditions, caused by high heat flow due to the presence of partial melt beneath the rift valleys in the region [Gass, 1970; Keir et al., 2011]. We use $M_L$ estimates to calculate the seismic moment release using empirical relationships, e.g., Kanamori [1977], following the method of Keir et al. [2011].

We computed lower hemisphere focal mechanisms to constrain the orientation of crustal strains using FOCMEC [Snoke, 2003]. The program uses the station location, take off angles, and $P$ and $S$ wave polarities to perform a grid search for the best-fit double-couple solution [Snoke, 2003; Ebinger et al., 2008]. Using an incremental step of 10°, all fault plane solutions have an error of ≤ ± 20° in strike and dip of the nodal planes. We were able to estimate 46 robust fault plane solutions beneath Nabro’s caldera. We could not determine solutions for events away from the caldera due to the configuration of seismic stations. Data from the seismic station with a failed GPS system (NAB7) were included in the dataset as the arrival time of the wave was not relevant for this analysis, but the position of the station was useful for determining the strike of the nodal planes.

3.3. Results
3.3.1. Spatial Variations

All of the events recorded can be defined as volcano-tectonic (VT) earthquakes as they have clear $P$ and $S$ wave arrivals, with an average peak frequency of 7 Hz [Lahr et al., 1994]. VT earthquakes are commonly recorded at preeruption, coeruption, and posteruption and can indicate changes in the magmatic plumbing
Figure 7. (a) Magnitude of 650 Hypo2000 located earthquakes over the 38 day recording period. (b) Cumulative seismic moment release of all earthquakes over the recording period. (c) Cumulative seismic moment release with the largest event removed. (d) Cumulative seismic moment for earthquakes under Nabro only.

system and emplacement of new intrusions [Hill, 1977; Umakoshi et al., 2001; Roman and Cashman, 2006; Roman et al., 2006]. Event locations after relocating with HypoDD are overlain on the Hypo2000 results (Figure 5). The relative error of the relocated earthquakes is ± 40 m in depth and ± 16 m in the horizontal coordinate. The depths are referenced to 700 m asl, the lowest elevation seismometer. Five clusters are visible in the spatial distribution of the earthquakes (Figure 5): (1) Directly beneath the vent, there is an elongate, subvertical cluster extending between 1 and 4 km depth. (2) The cluster is located beneath the central and southern part of the caldera, it is subhorizontal with the seismicity deepening to the SW, the cluster is ~5 km long and between 4 and 5 km deep. (3) Beneath the NE flank of Nabro, there is a NE striking cluster which deepens to the north, it is 6–11 km deep. (4) Beneath the SE caldera wall, 16 earthquakes are between 10 and 12 km deep. (5) A cluster lies directly beneath Mallahle, the hypocenters form a spherical cluster ranging between 4 km and 7 km deep. There is a noticeable aseismic zone between Nabro and Mallahle calderas. We will use these clusters to interpret fault slip induced by magma movement, highlighting potential magma pathways, as well as slip on larger scale preexisting faults induced by volume changes in magma reservoirs.

3.3.2. Magnitudes
We determined local magnitudes ($M_L$) to range between −0.37 and 4.5, for all 658 earthquakes located using Hypo2000. The magnitudes of the relocated earthquakes are shown in Figure 5. The majority of earthquakes beneath Mallahle have a magnitude between 1 and 2, (Figure 6). Most of the events with a magnitude between 0 and 1 are located beneath Nabro, but this can reflect bias caused by the station distribution. In order to see how magnitudes are distributed and how they establish cutoff magnitudes, we used the frequency-magnitude distribution (FMD) [Gutenberg and Richter, 1944]:

$$\log N = a - b M_c,$$

where $N$ is the cumulative number of earthquakes with a magnitude equal to or greater than $M$, $a$ is a constant describing the rate of seismic activity in the study area, and $b$ is the gradient of the FMD plot. $M_c$, also known as the “cutoff” magnitude, is the smallest magnitude of earthquake to which the catalog is complete; this is determined by the network sensitivity. As equation (1) uses only the maximum observed magnitude, the resulting $b$ value tends to be too low [Bender, 1983]. Therefore, as our data only spans a short period, we use the maximum likelihood formula (2) as derived by Utsu [1965] to calculate the $b$ value,

$$b = \log_{10} e \frac{M_a - M_c}{M_c}.$$
where $M_a$ is the average magnitude and $M_c$ is the cutoff magnitude. Previous works by Bridges and Gao [2006] and Sanchez et al. [2004] show how spatial variations in $b$ values can provide constraints on the distribution of magma in the subsurface. Therefore, we find separate $b$ values for the events on Nabro and those on Mallahle. We plot the FMD for Nabro and Mallahle events separately (Figure 6). The $b$ value was determined for Nabro using values of $M_a = 1.86$ and $M_c = 1.52$ and for Mallahle using $M_a = 2.62$ and $M_c = 1.82$. For all detected seismicity on Nabro, $b = 1.3 \pm 0.08$ for the events beneath Mallahle, $b = 0.97 \pm 0.15$ (Figure 6). The difference in cutoff magnitude between the two calderas is due to the siting seismic stations solely on Nabro. The seismic energy release will be compared to the accumulation of the seismic moment as determined by InSAR.

### 3.3.3. Temporal Variations

The daily number of earthquakes (Figure 7a) varies between 4 and 33 during the 38 day recording period. Figure 7b shows the original 658 earthquakes, which contribute $7.6 \times 10^{15}$ N m of seismic energy release. The largest release of seismic energy can be attributed to an event with a magnitude $> 4$. When this event is removed from the analysis (Figure 7c), it can be seen that the seismic moment release increases by between 0.2 and $0.4 \times 10^{15}$ N m steps every 6–10 days with a linearly increasing moment release between each step. These linear increases with discrete steps are observed on both Nabro and Mallahle calderas. Figure 7d shows the seismic energy release from the events on Nabro only, these show the same trend as that observed in Figure 7c. There appears to be no consistent temporal pattern in the spatial distribution of events.

### 3.3.4. Focal Mechanisms

We computed 46 focal mechanisms beneath Nabro’s caldera of which six were normal, 33 were thrust, and four were largely strike-slip motions (Figure 8). A prominent feature is a series of 18 thrust mechanisms with nodal planes striking NE-SW located in the center of the caldera, under the vent, which occur throughout the recording period at a depth between 4 and 5 km (Figure 8 [highlighted in bold], and Figure 9). In this region, there are three thrust mechanisms with differently orientated nodal planes; one striking northward and two with nodal planes striking ESE-WNW. Also in the center of the caldera, only one solution indicates normal faulting, the nodal planes strike SE-NW. Away from the center of the caldera, only nine of the 46 focal mechanisms have a major normal faulting component, four of which are located within the deep seismic cluster 4 (Figure 5). Due to the seismic network configuration, the focal mechanism of events beneath Mallahle caldera could not be constrained.

### 3.3.5. Waveforms

In order to test whether different earthquakes located close to each other are generated by the same slip motion in the same fault, we use the criteria of waveform similarities of earthquake pairs. Earthquake waveform pairs that have a significant similarity, expressed by a correlation coefficient greater than 0.7, are produced by the same source mechanism [Pechmann and Kanamori, 1982] and located within a distance of a 1/4 wavelength of each other [Geller and Mueller, 1980]. We can also use the correlation coefficients to qualitatively highlight changes in the subsurface. We have chosen two pairs of waveforms to perform the cross correlation, whose hypocenters are located within 215 m of each other, which is a 1/4 wavelength...
distance for these waveforms and all have the same focal mechanism. The first waveform pair are separated by 22 days, whereas the second pair occurs almost simultaneously, just 10 min apart. These four seismic waveforms have a peak frequency of approximately 7 Hz and contain some higher-frequency noise, which we filtered by applying a bandpass filter with corner frequencies of 2 and 10 Hz (Figure 10). We determined a cross-correlation coefficient of 0.20 and 0.84 for the first and second pairs, respectively. This discrepancy indicates that despite a close source location and the same focal mechanism, the path effects between the source and the receiver changed significantly between the two earthquakes constituting the first pair. This leads us to suggest that the subsurface evolved over the recording period, due to the ongoing subsidence.

4. Discussion

4.1. Joint Interpretation of InSAR and Seismicity

In this study we have measured the crustal response to the 2011 eruption of Nabro volcano. Using the high-resolution InSAR data in conjunction with seismicity, we are able to create a working model of the magmatic plumbing system and how it interacts with faults (Figure 11). We observe a circular subsidence signal which is offset to the SW of the caldera topography and the vent region, suggesting that the magma reservoir is not located directly beneath the eruption center. The subsidence signal suggests ongoing depressurization of the magma chamber following the eruption. The spatial pattern and sporadic nature of the hypocenters located at shallow depths (less than 6 km) under Nabro, are likely caused by the bending and episodic fracturing of brittle rocks within the volcanic edifice [Dzurisin et al., 1991, 2002], in response to the depletion of the magma chamber. The temporal pattern of earthquake hypocenters has previously been used to show the migration of magma preceding and during eruptions [Tarasewicz et al., 2012a]. However, beneath Nabro the seismicity recorded by the local array does not necessarily show this migration of magma to the surface, rather the constant reactivation of already developed faults, which slip during subsidence.

We find that the depth of the magma body, estimated by inverting the InSAR deformation field, is dependent on whether we chose a Mogi or sill source and the volume change imposed. The Mogi solution suggests a depth of 6.9 ± 1.1 km, whereas the sill solution yields a depth of 11 ± 2 km. Using the spatial distribution of the hypocenters, we suggest that the most applicable geometry of the source resembles the Mogi solution, as we interpret seismic cluster 2 (Figure 5) as the region of brittle failure immediately above the magma chamber, which fractures to accommodate the volume change. Therefore, the residual magma body is situated in the shadow zone immediately below this cluster. However, it is likely that the Mogi approximation is an oversimplification of the geometry of the magma source. A magma plumbing configuration of stacked sills was inferred from joint analysis of seismic, petrological, and geodetic data for Dabbahu volcano [Field et al., 2012]. The magma reservoir under Nabro may also constitute numerous lenses and dykes of partial melt across a depth range of 6 to 10 km, which together approximate a single point source ground deformation signal. The deep cluster of seismicity (cluster 4, Figure 5) directly beneath this region may be related to small-scale fracturing around a constricted part of the plumbing system, potentially linking the shallow sources to a deeper reservoir, similar to an interpretation of lower-midcrustal seismicity at
Figure 10. Examples of waveforms with a bandpass filter between 2 and 10 Hz applied. The hypocenters of the pairs are located within 215 m of each other. (a) Waveforms of earthquakes temporally separated by 22 days, with cross correlation of 0.20. (b) Waveforms of earthquakes temporally separated by 10 min, with cross correlation of 0.84.

Figure 11. Working model of the magma plumbing system beneath Nabro. (a) Map view of the observed subsidence from the ascending InSAR data. Black outlines: caldera rim and lava flow. Red dashed line: vent region. Black dots: relocated hypocenters. Red star: Mogi model center. Yellow rectangle: NE-SW thrust fault outline at the surface. (b) Three-dimensional view of the proposed working model. Top plane: the observed subsidence from the ascending InSAR data draped on topography. Lower volume: hypocenter locations at depth. Red: earthquakes induced directly by the eruption. Black: regional earthquakes induced by changes to the stress field. The proposed Mogi source (dark red spot), conduit (large black arrow), thrust fault (grey plane), and potential magma supply system (small black arrow) are also highlighted.
Mallahle, which implies that there is no current subsurface magmatic connection between the two calderas. Therefore, the seismicity we observe is due to changes in the stress field resulting from the subsidence at Nabro and not caused by magma movement beneath Mallahle. However, a connection between the two calderas may have existed in the past. Also, the large magnitude (M < 4) VT earthquakes which occurred beneath Mallahle suggest that preexisting faults have been brought closer to failure, due to stress changes following the magma reservoir depressurization [Wauthier et al., 2013a] We interpret seismic cluster 3 to also be a result of the stress change, where the linear structure implies a fault which has been created or reactivated due to the new distribution of stress. We can not constrain the focal mechanisms of these events as they are located outside of the local seismic array. Also, as the earthquakes which highlight the fault have a maximum magnitude of 2 and are at a depth of ~8 km, even if we assume the fault to have a 90° dip and a thrust mechanism, the surface deformation associated with this inferred structure is less than 0.5 mm. Therefore, it is not observable using InSAR techniques despite good coherence in this area. As this fault plane is very speculative we have not included it in the working model (Figure 11).

4.2. Modes of Caldera Subsidence
The structure and evolution of calderas provide information on the behavior magma reservoir, and therefore, understanding their geometries is crucial in predicting future behavior [Cole et al., 2005; Acocella, 2007]. We can compare the mode of subsidence implied by the focal mechanisms to models of caldera response. The seismic data reveal fault structures in the shallow subsurface (less than 6 km deep), the magnitudes of the earthquakes which delineate the fault have a maximum magnitude of 3. Earthquakes of this size at ~ 5 km depth cause less than 1 mm of deformation at the surface, which is not resolvable in the InSAR data. We also assess the temporal evolution of these faults through interpretation of the cross-correlated waveforms. In Figure 9, a thrust fault is observed to crosscut the caldera floor 1 km above the center of the magma source. Since the focal mechanisms define a 45° dip along one of the nodal planes (Figure 9), we infer that a fault plane strikes NE-SW, dipping 45° to the SE. We can compare this faulting to both numerical modeling performed by Holohan et al. [2011] and analog models [Lavallée et al., 2004; Kennedy et al., 2004; Roche et al., 2000] to provide further insights into the mechanisms of subsidence. Holohan et al. [2011] used a two-dimensional finite element method to model the caldera subsidence in a half space with a range of geomechanical properties. If we qualitatively compare Figure 9 to Figure 5c in Holohan et al. [2011], we find similarities such as the dip and motion of the fault plane and its position relative to the magmatic body. Using the terminology of Holohan et al. [2011], our results could also be described as “reverse fault that separates two inward rotated roof blocks.” Quantitatively, the model we refer to would require the ratio between the thickness and diameter of the roof to be less than 0.33. Assuming that the seismicity under Nabro highlights the brittle failure of the roof, we find this ratio is between 0.69 and 0.88. As Nabro’s caldera is already well established, the fault plane we observe may have existed prior to the eruption and has been reactivated. This may explain the presence of the fault despite the higher ratio between the thickness and diameter of the roof. Furthermore, we observe a linear increase in the seismic energy release interrupted by discrete steps on a week time scale at Nabro, which is consistent with the findings of Ruch et al. [2012] that incremental collapses can occur on mature faults during caldera collapse. In the absence of appropriate measurements for bulk porosity, bulk density, and Youngs modulus for rocks at Nabro, the benefit of further quantitative application models such as that of Holohan et al. [2011] is limited.

Ring faults are a common feature of a caldera collapse [Marti et al., 1994; Cole et al., 2005]. However, the hypocenters we located are not concentrated on the caldera walls, implying that these structures may not have been activated during the eruption, which is not uncommon [Kennedy et al., 2004]. In addition, the fault plane solutions of those found in the vicinity of the caldera walls are not tensitional (Figure 9). The modelling by Holohan et al. [2011] shows an upward migration of faulting; therefore, the hypocenter locations are expected to migrate toward the surface over time. However, as no such pattern is observed within seismic cluster 1, the faults are assumed to have been formed before the local seismic array was deployed, and we only observe their sustained reactivation as the caldera relaxes. By comparing the waveforms of two pairs of earthquakes with adjacent hypocenters on the same fault plane but with each pair having a different temporal separation, we find a distinct decrease in correlation over time. This suggests that subsurface structures were evolving even during the recording period.

4.3. The b Values
The b values describe a region’s ability to accumulate stress, and the average global b value is approximately 1.0 [Richter, 1958]. However, b values can vary between regions as different geomechanical properties...
influence the ability of rock to accumulate stress. Low b values indicate that a region is capable of accumulating significant stresses, which can result in large earthquakes. Areas with an increased thermal gradient [Warren and Latham, 1970] can be associated with a weak rheology, which cause small magnitude stress changes that tend to favor small-magnitude earthquakes. The lower b value for Mallalhe implies that the earthquakes generated under Mallalhe caldera are not dominated by magmatic processes and occur in rock with a stronger rheology. This is consistent with our conclusion that there is no subsurface magmatic link between Nabro and Mallalhe calderas. The b value we calculated on Nabro is higher, likely due to a relatively weaker rheology, the presence of fluids and melt, the presence of highly fractured rock typical of heavily faulted calderas, and a higher geothermal gradient associated with the magma reservoir.

4.4. Off-Rift Volcanism

Off-rift volcanism is a common phenomenon that has also been observed in the Virunga Volcanic Province [Ebinger, 1989], in the Red Sea rift [Bosworth et al., 2005], Iceland [Sturkell et al., 2003], and the Baikal Rift [Kiselev, 1987]. Above the rift axis of the ARZ lie large volcanic provinces constructed from magma generated by decompression melting due to lithospheric thinning [Hammond et al., 2013]. Pagli et al. [2012] suggest that an elevated magma supply in the rift axis of northern Afar results in shallow magma chamber depths, for example, the < 2.5 km depth chambers determined under Alu-Dalafilla and Dallol volcanoes [Pagli et al., 2012; Nobile et al., 2012]. Our results show that the magma plumbing system of the off-rift, flank volcanoes of the Danakil depression are fundamentally different from those in the rift axis and have deeper magma chamber depths. This is consistent with a lower spreading rate and thicker crust [Purdy et al., 1992; Morgan and Chen, 1993; Chen and Morgan, 1996].

In rift settings the regional maximum compressive stress is vertical [Illies, 1981; Bosworth et al., 1992]. On Nabro we expect the regional stress field to produce a vertical P axis and a NE striking T axis. However, our post-eruption focal mechanisms show a horizontal NW striking P axis, revealing a local 90° shift from the expected regional orientation. Studies of VT earthquake swarms have documented a ~90° rotation of the P axis on volcanoes prior to and during eruptions, due to the propagation or inflation dikes [Roman and Cashman, 2006; Lehto et al., 2010]. However, on Nabro we find that the 90° shift is present during the post-eruptive episode, while the volcano is subsiding, the NE-SW striking thrust fault is the geological expression of this stress field. We propose that this post-eruption rotation observed on Nabro is due to the stress field induced by magma reservoir depressurization [Vargas-Bracamontes and Neuberg, 2012]. However, the fault geometry may also be influenced by the geomechanical structure of the caldera as well as changes to the magmatic plumbing system.

The NVR strikes oblique to the Red Sea rift, bisecting the Danakil microplate which is considered a relatively unriifted, coherent block [McClusky et al., 2010; Hammond et al., 2013]. Hammond et al. [2013] suggest that a thermal anomaly may be present, and some argue that increased melt production coincides with steep gradients in the lithosphere-asthenosphere boundary [Holtzman and Kendall, 2010; Rychert et al., 2012]. However, these arguments do not explain the strike and extension of the NVR as a near continuous lineament from the ARZ to the Red Sea. Barberi et al. [1974] hypothesized that the NVR is a transverse structure, which developed through the rejuvenation of tectonically weak zones that proceeded rift formation. The global CMT catalog shows that the majority of magnitude >4 earthquakes along the NVR have strike-slip and normal fault mechanisms. In addition to fault slip and style, the NEIC catalog of earthquakes shows that the NVR is also well delineated by NE-SW striking alignment of earthquakes. The combination of fault slip style and earthquake locations on a regional scale show that the NVR has a transtensional motion, somewhat consistent with the previous interpretation in Barberi et al. [1974]. In addition, all of our focal mechanisms, which we use to constrain the NE-SW thrust fault crossing the caldera floor, have a strike-slip component. The orientation and strike slip could be due to a preexisting structural grain created by regional transverse motions, which was subsequently exploited during subsidence [Holohan et al., 2008]. At Nyamulagira volcano a crosscutting caldera fault has also been observed during intereruptive periods, and it is considered to be a result of regional stresses [Wadge and Burt, 2011; Toombs and Wadge, 2012; Wauthier et al., 2013b]. However, on Nabro we cannot differentiate between this cause of strike-slip motion and that produced by the caldera collapse itself. Horizontal motions caused by the interactions of numerous faults on the caldera floor can produce oblique slip faults [Holohan et al., 2013]. The global CMT catalog of normal fault mechanisms and presence of volcanoes along the line suggest that the transform motion is accommodated by opening, partly accommodated by magma intrusion. Joint geological and geophysical data therefore show that the NVR may be analogous to a “leaky” transform fault, common on the magma-rich
ocean ridge system [Gregg et al., 2007]. Our interpretation has the implication that the Danakil block may experience internal deformation and may be better approximated as two microplates either side of the NVR.

5. Conclusions

Our InSAR analysis of ascending and descending images, acquired after the eruption by the TSX satellite between 1 July 2011 and 10 October 2012, shows a concentric subsidence signal centered on Nabro’s caldera with a maximum rate of 20 cm/year. The InSAR data can be modelled as a Mogi source at a depth of 6.9 ± 1.1 km. However, this may be an oversimplified model of magma reservoir geometry. We located 658, and relocated 456 earthquakes recorded over a 38 day period beginning on 31 August 2011. From the distribution of seismicity, we observe fracturing of brittle rock above the magma chamber. In conjunction with focal mechanisms, we delineate a major fault plane with a NE-SW strike which dips 45° to the SE, crosscutting the caldera floor. A deep cluster of seismicity suggests a link to a deeper magma source. The b value of the earthquakes beneath neighboring Mallahle volcano and the circular subsidence signal centered on Nabro, suggest that there is no subsurface magmatic link between Nabro and Mallahle calderas.

We observe a reverse fault which cuts through the center of the caldera floor and has the same NE-SW strike as the NVR. This mode of subsidence has been referred to as "snap style" [Holohan et al., 2011]. In addition, this fault contains a strike-slip component, which is probably the result of a regional structural grain. The magma reservoir beneath Nabro is deep and this is only the second eruption of an off-rift volcano associated with the ARZ in modern times. We suggest that this is due to a low magma supply rate beneath Nabro in comparison to the volcanic centers on the rift axis. The majority of the subsidence is accounted for by the Mogi model. The seismicity represents minor deformation and is not required to account for the subsidence. Our results show that the post-eruption subsidence of the caldera is controlled by the changes associated with the magma reservoir rather than significant slip on caldera ring faults, which were not activated during the post eruption phase that we have studied.

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References


