# Lateral variation of Lg wave propagation in southern Mexico

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Received 20 September 2000; revised 30 January 2001; accepted 19 August 2001; published 17 January 2002.

[1] In this study we investigated lateral variation of Lg wave propagation in southern Mexico from recordings of 92 crustal earthquakes along 591 travel paths. The efficiency of Lg propagation was measured in terms of Lg to Pn spectral ratio. It was found that Lg propagation is inefficient for travel paths through the Gulf of Mexico coastal plains and the Gulf of Tehuantepec, areas with thick layers of sediments. An average Lg quality factor,  $Q_{Lg}$ , as a function of frequency for southern Mexico was estimated for the efficient Lg travel paths. The relation obtained for  $Q_{Lg}$  in the frequency range 1.6–8 Hz is  $Q_{Lg}(f) = 204 f^{0.85}$ . The lateral variation of  $Q_{Lg}^{-1}$  was solved as a mixeddetermined inverse tomography problem, separately for each frequency, in which a spatial smoothness constraint was imposed and a priori information was added in poorly covered regions. The spatial resolution obtained was about 200 km. It was found that the Trans-Mexican Volcanic Belt, the Gulf of Mexico coastal plains, and the area east of 94°W are characterized by lower than average  $Q_{Lg}$  values, i.e., higher attenuation. High  $Q_{Lg}$  values were obtained for the Mixteco-Oaxaca terranes, while for the Guerrero terrane, values similar to the average were obtained. The results show a correlation between  $Q_{Lg}$  and crustal structure and provide valuable information on lateral variation of  $Q_{Lg}$ , which is needed for reliable prediction of ground motion during future earthquakes. INDEX TERMS: 7205 Seismology: Continental crust (1242), 8180 Tectonophysics: Tomography, 9350 Information Related to Geographic Region: North America

## 1. Introduction

[2] The tectonic structure of southern Mexico is characterized by an aggregate of several blocks that are bounded by faults. Campa and Coney [1983] proposed a division of southern Mexico into several tectonostratigraphic terranes (Figure 1): Xolapa, Oaxaca, Mixteco, Zapoteco, Maya, and Guerrero. The composition and tectonic evolution of these terranes were broadly explained by Sedlock et al. [1993]. For the purpose of the present work we differentiate between two types of terranes, those with cratonic basement such as the Oaxaca and Zapoteco terranes, and those formed from collision tectonics such as the Xolapa, Juárez, Mixteco, and Guerrero terranes. The latter terranes consist of sediments and/or oceanic rocks that collided with continental blocks and were later deformed and intruded. The Trans-Mexican Volcanic Belt (TMVB) is composed of late Miocene to present andecitic and dacitic deposits. The Gulf basin is considered to be a passive margin with a large accumulation of sediments and salt tectonics. A knowledge of the crustal and upper mantle structure in Mexico is important for understanding the tectonic evolution of this region as well as for the estimation of ground motion during future earthquakes. Since the pioneering study by Meyer et al. [1961] the velocity structure of the crust and upper mantle below central and southern Mexico has been the subject of numerous studies [e.g., Fix, 1975; Valdés et al., 1986; Gomberg and Masters, 1988; Nava et al., 1988; Campillo et al., 1996; Shapiro et al., 1997].

[3] The quality factor, describing attenuation of seismic waves, is one of the basic parameters characterizing Earth's crust. It depends on the type of rocks and the degree of heterogeneity and therefore is correlated with the geological structure. Several studies of attenuation and its regional variation in southern Mexico have been carried out over the last decade. An overview of these studies and their results is given in Table 1. Figure 2 shows the regions studied in previous works. Castro et al. [1990] determined *Q* from *S* waves recorded at distances up to 133 km along the Guerrero subduction zone by simultaneously inverting for site response, O, and source spectra. Ordaz and Singh [1992] studied source spectra and spectral attenuation of crustal events in the subduction zone recorded in Guerrero and the Valley of Mexico. They obtained a frequency-dependent quality factor, Q(f) = 273, which may be taken as a reference value for southern Mexico. Castro and Munguía [1993] found a lower quality factor for S waves above the Oaxaca subduction zone. Castro et al. [1994] compared results for Q from Oaxaca and Guerrero and attempted to explain the unexpected lower Q in the Oaxaca region. Domínguez et al. [1997] studied the regional variation of attenuation of Lg waves between Guerrero and Oaxaca. They used travel paths between Guerrero/Oaxaca and Veracruz at the Gulf of Mexico. Yamamoto et al. [1997] described the lateral variation of Lg coda Q in southern Mexico based on events, including subcrustal events, from the subduction zone and recorded at a single station in the Valley of Mexico. They observed a higher Q value for the Michoacan-Jalisco and Oaxaca regions as compared with Guerrero. However, they reported an even higher O value for the volcanic belt, which seems unreasonable. More efficient propagation for paths going inland as compared with paths going parallel to the coast had been suggested by Singh et al. [1988]. Cárdenas et al. [1998] investigated these differences in attenuation between paths along and perpendicular to the coast using data

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Figure 1. Main geologic units of southern Mexico.

from a seismic refraction experiment. They found lower average attenuation for the travel paths going inland.

[4] The previous Q studies for southern Mexico described localscale attenuation based on small data sets. In southern Mexico it is possible that various tectonic provinces will be reflected in lateral variation of Q on a regional scale. We took advantage of the availability of a large, high-quality data set to study the lateral variation of Q in southern Mexico on a regional scale. This is the first study for southern Mexico that attempts to resolve regional variation of Q caused by large variations in crustal structure. Since Lg waves propagate in the crust and are observed over a large distance range, Q can be reliably determined from the decay of Lgspectral amplitudes with distance [e.g., Campillo, 1987; Baumont et al., 1999]. The Q variation in this study is solved as a tomography problem. However, before performing a formal inversion, the efficiency of Lg wave propagation was quantified in terms of the spectral ratio of Lg to Pn, and an average Q value for southern Mexico was determined.

[5] The propagation of Lg waves as one of the dominant phases at regional distances was first described by Press and Ewing [1952]. The Lg waves have been modeled as higher-mode surface waves [Herrmann and Kijko, 1983] or as multiple reflected S waves [Campillo et al., 1984; Campillo, 1990], which propagate in the crust. The characteristics of the propagation of Lg waves have been discussed for many regions [e.g., Ruzaikin et al., 1977; Campillo and Plantet, 1991; Campillo et al., 1993; Chazalon et al., 1993; McNamara et al., 1996; Shi et al., 1996; Benz et al., 1997; Rial and Ritzwoller, 1997; Rodgers et al., 1997; Mellors et al., 1999; Calvert et al., 2000] and have been studied using numerical simulations [e.g., Kennett, 1986; Maupin, 1989; Regan and Harkrider, 1989; Cao and Muirhead, 1993; Gibson and Campillo, 1994; Furumura and Kennett, 1997, 1998; Vaccari and Gregersen, 1998]. It has been observed that Lg propagation becomes inefficient or is blocked if the crustal structure undergoes fast lateral changes [Ruzaikin et al., 1977; Baumgardt, 1990; Campillo et al., 1993; Chazalon et al., 1993] or if the travel path crosses oceanic crust [Press and Ewing, 1952; Knopoff et al., 1979;

Kennett et al., 1985; Gregersen and Vaccari, 1993; Shapiro et al., 1996]. The lateral variation of coda *Q* has been determined on the basis of *Lg* coda [e.g., *Singh and Herrmann*, 1983; *Xie and Mitchell*, 1990]. Source characteristics have also been determined from the analysis of *Lg* waves [e.g., *Hasegawa*, 1983].

## 2. Data

[6] The network of broadband stations operated by the National Autonomous University of Mexico (UNAM) provided the highquality, three-component broadband data used in this study. Most of the broadband seismic stations are located in southern Mexico. All stations are equipped with STS-2 sensors and a 24-bit Quanterra acquisition system, except for station TEIG, which is equipped with a Geotech KS-36000-I borehole seismometer (50-s natural period). The stations and the epicentral locations used in this study are shown in Figure 3. Seismicity is highest in the subduction zone along the Pacific coast of Mexico. Lg waves are most efficiently excited by earthquakes in the continental crust. Therefore only crustal earthquakes, with depths of less than 35 km, were selected from the area between  $13-24^{\circ}N$  and  $94^{\circ}-108^{\circ}W$ . Locations were taken from the catalogue of the National Seismological Service (SSN). Since the depths are not well constrained, the records were visually checked for the presence of crustal phases to eliminate noncrustal events. The magnitude range was chosen between 4.5 and 6.7. An upper magnitude limit was used to avoid the effect of source complexity on the Lg wave propagation. It was required that the events be recorded by at least four stations. The minimum epicentral distance was set to 200 km to ensure a clear observation of Lg waves. The selected earthquakes were from the period October 1995 to June 2000: a total of 92 events with 591 travel paths (Figure 4). It is seen that the highest path density was obtained between the Pacific coast and central southern Mexico. The average group velocity of the Lg peak amplitude was found to be 3.35 km s<sup>-1</sup>, and therefore the Lg group velocity window was selected between 3.0 and 3.7 km s<sup>-1</sup>. The Pn group velocity window was selected between 6.5 and 8 km  $s^{-1}$ .

# 3. Efficiency of Lg Waves

[7] We characterized the efficiency of the Lg wave propagation by the spectral ratio of Lg to Pn waves. Since Pn propagation is less dependent on the lateral variations in the crustal structure as compared to Lg, this ratio provides an adequate measure of the efficiency of Lg propagation. Measuring the efficiency of Lgpropagation in terms of Lg/Pg or Lg/Sn would be less valuable, since Pg is expected to show a similar attenuation pattern as Lg and Sn are expected to be extremely variable in volcanic regions. Contamination of Lg by Sn coda, as, for example, observed by *Shin* and Herrmann [1987] in Canada for distances larger than 500 km and frequencies above 7 Hz, was found to be negligible in Mexico.

 Table 1. Overview of Results From Previous Studies of Attenuation in Southern Mexico

Reference	Type of Wave	Region	Distance Range, km	Frequency Range, Hz	Geometrical Spreading	Results
Castro et al. [1990]	S	Guerrero	13-133	0.1 - 40	$\frac{1/R}{(1/R)^{0.5}}$	$Q_S(f) = 278 f^{0.92}$ $Q_S(f) = 96 f^{0.96}$
Ordaz and Singh [1992]	S	Guerrero-Mexico City	<323	0.2-10	$\frac{1/R \text{ for } R \leq R_x;}{(R_x R)^{-0.5} \text{ for }}$	$\tilde{Q}_S(f) = 273 f^{0.66}$
Castro and Munguia [1993]	P and $S$	Oaxana	19-76	1.0-25	$\frac{1}{(1/R)^{0.5}}$	$Q_S(f) = 56 f^{1.01}$ $Q_P(f) = 22f^{0.97}$
Domínguez et al. [1997]	Lg	Oaxana Guerrero	285-640	2.0 - 7.0	$(1/R)^{0.883}$	$Q_{Lg}(f) = 59f^{0.81}$ $Q_{Lg}(f) = 134f^{0.83}$
Yamamoto et al. [1997]	Lg Coda	Oaxana Michoacan-Jalisco Guerrero	155-520	0.2-2.0		$ \widetilde{Q}_{Lg}(f) = 190f^{0.7}  Q_{Lg}(f) = 195f^{0.75}  Q_{Lg}(f) = 178f^{0.65} $



**Figure 2.** Regions investigated in previous *Q* studies for Mexico. (a) Area 1 studied by *Castro and Munguía* [1993], area 2 studied by *Castro et al.* [1990] and *Ordaz and Singh* [1992], and area 3 studied by *Cárdenas et al.* [1998]; (b) Guerrero (denoted by G) and Oaxaca (denoted by O) sectors studied by *Domínguez et al.* [1997]; and (c) Michoacan-Jalisco (M), Guerrero (G) and Oaxaca (O) sectors as defined by *Yamamoto et al.* [1997].

[8] For each source-receiver path the time windows corresponding to the respective group velocity windows for Lg and Pn waves were extracted, the average Fourier spectral levels around a selected center frequency were determined, and the spectral ratios of Lg to Pn waves were computed. It was required that the Pnspectral level be higher than twice the spectral level of the noise. We regarded an Lg to Pn ratio of below 3 as inefficient, 3 to 6 as intermediate, and above 6 as efficient. An example of efficient Lgpropagation is shown in Figure 5. Figure 6 shows the difference between efficient and inefficient travel paths. The travel path to station TEIG, which crosses the sedimentary basin at the Gulf of Mexico shows inefficient Lg propagation. At lower frequencies, no Lg waves were seen in the seismogram for TEIG, indicating that the inefficiency is due to attenuation and not to mode conversion from Lg to Sn waves. Domination of Sn coda over Lg for this travel path toward higher frequencies was not observed.

[9] Figure 7 shows the efficiency of Lg wave propagation for all travel paths at 2 Hz. It is seen that all travel paths to TEIG are inefficient. Strong Lg attenuation can be caused by high anelastic attenuation, enhanced scattering of S waves, or structural effects. For example, it has been suggested that crustal thinning or strong variation of the Moho topography can result in a significant Lg attenuation [e.g., *Kennett*, 1986; *Campillo*, 1987; *Campillo et al.*, 1993]. Lg waves can also be strongly attenuated or blocked by sedimentary basins [e.g., *Knopoff et al.*, 1979; *Zhang and Lay*, 1995; *Shapiro et al.*, 1996]. In this case a large part of the Lg energy becomes trapped in shallow sedimentary layers where attenuation is high. We believe that the latter mechanism is responsible for the inefficient Lg propagation along the paths crossing large sedimentary basins, i.e., (1) the Gulf of Tehuantepec and (2) the Gulf of Mexico coastal plain [*Guzman*, 1962].

[10] It is important to note that the Lg/Pn ratio not only reflects Lg efficiency but also depends on the characteristics of Pn. In general, Pn is an extremely variable phase in terms of amplitude. Also, the difference between Lg and Pn in geometrical spreading and dependence on the radiation pattern will effect the Lg/Pn ratio. In spite of these difficulties the Lg to Pn spectral ratio provides a rough measure of the efficiency of Lg wave propagation. Figure 7 is in agreement with observations from seismograms that show Lg inefficiency and it is seen that lateral changes in crustal structure such as the sedimentary basin near the Gulf coast are reflected in the Lg propagation pattern. The Lg/Pn ratio was used as criteria to exclude inefficient paths from the determination of the average  $Q_{Lg}^{-1}$ .

# 4. Determination of Average $Q_{Lg}$ in Southern Mexico

[11] The main goal of this study was to determine the lateral variation of the quality factor  $Q_{Lg}$ . However, for practical purposes of estimating ground motion and to provide an a priori estimate of  $Q_{Lg}$ , we first determined an average quality factor for southerm Mexico.

[12] The Lg wave displacement spectral amplitude  $A_{kl}(f)$  for the event k, at the recording site l, after removal of the instrument response, is given by

$$A_{kl}(f) = S_k(f)L_l(f)G(R) \exp(-\pi f R Q_{Lg}^{-1}/\nu).$$
(1)

where  $S_k(f)$  is the source term,  $L_l(f)$  is the local site term, R is the hypocentral distance, v is the average Lg peak velocity (3.35 km s<sup>-1</sup>),  $Q_{Lg}$  is the quality factor, and G(R) is the geometrical spreading, which is given by [*Herrmann and Kijko*, 1983]

$$G(R) = \begin{cases} R^{-1} & R \le R_x \\ (R_x R)^{-1/2} & R \ge R_x. \end{cases}$$
(2)

[13] This form of G(R) implies dominance of body waves for  $R \le R_x$  and of surface waves for  $R \ge R_x$ . Herrmann and Kijko [1983] showed that  $R_x$  is twice the crustal thickness, which in the region of interest is about 40–45 km. In this study we set  $R_x$  to be 100 km. Shin and Herrmann [1987] reported that the observed geometrical spreading of Lg waves in the time domain,  $R^{-0.83}$ , is equivalent to  $R^{-0.5}$  in the frequency domain. Taking the logarithm of (1) for distances larger than  $R_x$  gives

$$\log A_{kl}(f) + 0.5 \log(R_x R) = \log S_k(f) + \log L_l(f) - (\pi f R \log (e)/\nu) Q_{L_x}^{-1}.$$
 (3)



Figure 3. Station (triangles) and epicenter (circles) locations used in this study.

[14] As a constraint for the site terms we required that

$$\sum_{l} \log L_l(f) = 0.$$
(4)

[15] Equation (3) can be written in matrix formulation as

$$\mathbf{d} = \mathbf{G}\hat{\mathbf{m}}\,,\tag{5}$$

where **d** is the data vector, which is the left hand side of equation (3); **G** is the kernel matrix; and  $\hat{\mathbf{m}}$  is the estimated model vector. The estimated model contains the source terms, the site terms, and the average inverse quality factor  $Q_{Lg}^{-1}$ . The linear overdeter-

mined inverse problem was solved through singular value decomposition [*Menke*, 1989; *Press et al.*, 1986]. [16] In the determination of the average  $Q_{Lg}^{-1}$ , the inefficient

[16] In the determination of the average  $Q_{Lg}^{-1}$ , the inefficient travel paths that are not representative for central southern Mexico were omitted, which means that mostly travel paths from events in the subduction zone west of 96°W were used (Figure 8). The average  $Q_{Lg}^{-1}$  was determined for the vertical and horizontal components separately. The horizontal component was taken as square root of the squared spectral amplitudes from the E-W and N-S components. The results did not show any significant differences. The results for  $Q_{Lg}^{-1}$  presented here are derived from the vertical components.

[17] The dependence of Q with frequency is generally approximated [e.g., *Fedotov and Boldyrev*, 1969; *Aki*, 1980] by a power law in the form of



Figure 4. Travel paths showing the complete data set.

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$$Q_{Lg}(f) = Q_0 f^{\beta}. \tag{6}$$

[18] The frequency dependence obtained for  $Q_{Lg}^{-1}$  is shown in Figure 9. The relation for  $Q_{Lg}^{-1}$  in the frequency range 1.6–8 Hz is given by  $Q_{Lg}^{-1}(f) = 0.00489$  (±0.0006)  $f^{-0.85}$  (±0.089), which corresponds to  $Q_{Lg}(f) = 204 f^{0.85}$ . This result, considering the relatively large uncertainties, is in agreement with other studies, for example, *Ordaz and Singh* [1992]. Our result has been obtained from a larger data set and hence is valid for a larger part of southern Mexico. Below 1.6 Hz,  $Q_{Lg}^{-1}$  only shows minor changes with frequency and can be approximated by its value at 1.6 Hz. *Aki* 



**Figure 5.** Seismogram distance plots that show Lg propagation. The top map shows the travel paths. In the bottom plot, station codes are given on the left, and the numbers on the right side of the traces indicate the Lg to Pn spectral ratio at 2 Hz. The numbers above the traces and the lines show the group velocity windows. The seismograms are filtered between 1 and 5 Hz.



**Figure 6.** Example of inefficient *Lg* propagation to station TEIG. For details, see Figure 5.

[1980], on the basis of the comparison of frequency-dependent  $Q_S^{-1}$  at high frequencies (1–25 Hz) and  $Q^{-1}$  from surface wave measurements at long periods, postulated that  $Q_S^{-1}$  may have a peak value at around 0.5 Hz. Our observations (Figure 9) show a peak of  $Q_{Lg}^{-1}$  at around 1 Hz. This is an important result since it gives support to Aki's hypothesis on the basis of the analysis of a single wave type. The frequency dependence of  $Q_{Lg}^{-1}$  in the frequency range 1.6–8 Hz is expected to be mainly caused by the frequency dependence of scattering attenuation, while intrinsic attenuation is less frequency dependent [e.g., *Dainty*, 1981; *Mayeda et al.*, 1992].

[19] A difference in the attenuation for paths going parallel to the coast compared with paths going inland was observed by *Singh et al.* [1988] and *Cárdenas et al.* [1998]. To investigate this difference, the data set was divided into two groups of travel paths, parallel and perpendicular to the coast, and inverted for  $Q_{Lg}^{-1}$ independently. No significant difference was found. This result



**Figure 7.** Lg propagation efficiency at 2.0 Hz, estimated from Lg to Pn spectral ratio. The ratio range is given in the bottom left corner of each map. The events are grouped into inefficient ( $0 < ratio \le 3$ ), intermediate ( $3 < ratio \le 6$ ), and efficient (ratio > 6) Lg propagation.

means that on a regional scale, there is no evidence of the difference, which may exist on a smaller scale.

# 5. $Q_{Lg}$ Tomography

[20] A tomography study, based on a large, high-quality data set, can provide valuable information on the lateral variation of the quality factor Q [*Campillo*, 1987; *Baumont et al.*, 1999]. The tomography inverse problem is generally mixed determined; that is, while some model parameters are overdetermined, others are underdetermined [*Menke*, 1989]. Obviously, the problem of Q tomography in southern Mexico is mixed determined, since some areas have a high path coverage, while other areas are poorly covered. We follow the approach presented by *Barmin et al.* [2001], who described a fast and reliable method to solve two-dimensional tomography problems applying simple regularization conditions.

#### 5.1. Method

[21] The area of interest was divided into evenly spaced grid cells with a dimension of 1° in both N-S and E-W directions. Tests with different grid sizes were performed, giving very similar results. The attenuation term for a single travel path is given by exp  $(-\pi f v^{-1}((\Sigma R_i) Q_{Lg \ a \ priori}^{-1} + (\Sigma R_i \Delta Q_{Lg}^{-1})))$  where *i* is the grid cell index;  $R_i$  is the length of the travel path; and  $\Delta Q_{Lg}^{-1}$  is the difference from  $Q_{Lg \ a \ priori}^{-1}$ , the regional average obtained above, in the grid cell *i*. Equivalent to (3), we obtain

$$\log A_{kl}(f,R) + 0.5 \log (R_x R) +$$

$$\pi \left(\sum R_{i}\right) f \log (e) v^{-1} Q_{Lg \ a \ priori}^{-1} = \log S_{k}(f) + \log L_{l}(f) - (\pi f \log (e) v^{-1}) \sum (Q_{Lg \ i}^{-1} R_{i}).$$
(7)

[22] This system of linear equations again can be written in a matrix formulation as given in (5). The model vector now contains the  $\Delta Q_{Lg_i}^{-1}$  values instead of the average  $Q_{Lg}^{-1}$ . The data vector is modified from (3). The function that we minimize is of the form

$$(\mathbf{G}\mathbf{m} - \mathbf{d})^T \mathbf{C}_{\mathbf{d}}^{-1} (\mathbf{G}\mathbf{m} - \mathbf{d}) + \mathbf{m}^T \mathbf{A}\mathbf{m}, \qquad (8)$$

where  $C_d^{-1}$  is the data covariance matrix, which we set to the identity matrix, **I**, assuming that our data is uncorrelated. The dimension of the **G** matrix is  $M \times N$ . N is the number of travel paths, M is the number of all model parameters, and Y is the number of the  $Q_{Lg}^{-1}$  model parameters. In order to regularize the mixed determined problem the matrix **A**, with dimension  $M \times M$ , is added:

$$\mathbf{A} = \mathbf{F}^T \mathbf{F} + \mathbf{H}^T \mathbf{H}, \qquad (9)$$

[23] The **F** matrix adds spatial smoothness for the  $Q_{Lg}^{-1}$  model parameters, while **H** adds  $Q_{Lg}^{-1}$  a priori information for underdetermined grid cells. **F** is given as

 $V_{ij} = \exp\left(-R_{ij}^2 / 2\sigma^2\right)$ 

$$\mathbf{F}_{ij} = \begin{cases} \alpha & i=j\\ -\alpha V_{ij}/p_j & i\neq j, \end{cases}$$
(10)

where

and

$$p_j = \sum_{i=1, i \neq j}^{Y} V_{ij} \,. \tag{12}$$

(11)

[24] The damping constant  $\alpha$  was set to 500 and the spatial smoothing constant  $\sigma$  was set to 100. These values were selected by trial method to produce a smooth tomographic model with recognized tectonic patterns. Because of the **F** matrix the differences between spatially near grid cells will be minimized. The **H** matrix is defined as

$$\mathbf{H}_{ij} = \begin{cases} 0 & i \neq j \\ \beta \exp(-\lambda L_{ij}) & i = j, \end{cases}$$
(13)

where  $L_{ij}$  is the sum of all travel path segments crossing the grid cell *ij*. The damping constant  $\beta$  and the constant  $\lambda$  were set to 1000 and 0.001, respectively. These parameters were selected on the basis of visual analysis of the results, ensuring that the **H** matrix



Figure 8. Travel paths showing events and stations used for determining the average inverse quality factor.

adds a priori information only where the travel path coverage is low.

[25] The estimated model vector is obtained through

1

$$\hat{\mathbf{n}} = \tilde{\mathbf{G}}\mathbf{d}$$
 (14)

with

$$\tilde{\mathbf{G}} = \left(\mathbf{G}^T \mathbf{G} + \mathbf{A}\right)^{-1} \mathbf{G}^T.$$
(15)

[26] The model resolution matrix  $\mathbf{R}$  is given by

$$\hat{\mathbf{m}} = \tilde{\mathbf{G}}\mathbf{d} = \mathbf{G}\tilde{\mathbf{G}}\mathbf{m} = \mathbf{R}\mathbf{m}\,,\tag{16}$$

where **m** is the true model vector and  $\hat{G}$  is given by (15). To estimate the approximate spatial resolution, from each row of the resolution matrix **R** we computed the model spatial resolution for the cell *i* as

$$\mathbf{m}_{\mathrm{SR}}^{i} = \left(\sum_{j=1}^{Y} \mathbf{R}_{ij} r_{ij}\right) / \sum_{j=1}^{Y} r_{ij}, \qquad (17)$$

where  $\mathbf{R}_{ij}$  is the distance between grid cell *i* and *j* and  $r_{ij}$  is the element of the resolution matrix.

#### 5.2. Results

[27] In the inversion a tradeoff among  $Q_{Lg}^{-1}$ , the site term, and the source term is possible. This may be especially true for travel paths to TEIG, east of 96°W (Figure 7), because of low station coverage in this region. Initial inversions suggested that this was in fact so. For this reason, we fixed the site term at TEIG to 1, while requiring  $\Sigma log L_i(f) = 0$  for the remaining sites. TEIG is a hard limestone site, so that L(f) = 1 is reasonable. As shown in Appendix A, the source and the site terms estimated from the inversion are reasonable, giving confidence in our results on  $Q_{L_g}^{-1}$ .

[28] The tomography inversion was performed separately for 16 frequencies between 0.2 and 8 Hz. The results for  $Q_{Lg}^{-1}$ , the spatial



Frequency, Hz

**Figure 9.** Average inverse quality factor  $Q_{Lg}^{-1}$  as a function of frequency; data points obtained shown as circles with error bars corresponding to 1 standard deviation. The solid line is the linear least squares fit using data points between 2 and 8 Hz from this study; the dashed line shows the result of *Ordaz and Singh* [1992].



**Figure 10.** Results from the tomography inversion at various frequencies: (a)  $Q_{Lg}^{-1}$  at 0.5 Hz, (c)  $Q_{Lg}^{-1}$  at 2.0 Hz, and (e)  $Q_{Lg}^{-1}$  at 5.0 Hz. The spatial resolution and the travel paths at the respective frequencies: (b) 0.5 Hz, (d) 2.0 Hz, and (f) 5.0 Hz. The numbers and outlined areas in Figures 10a, 10c, and 10e show the regions defined through variation of  $Q_{Lg}^{-1}$ : 1 is Guerrero, 2 is Mixteco-Oaxaca, 3 is Trans-Mexican Volcanic belt (TMVB) near Popocatépetl, and 4 is Gulf coastal plains. The site term at TEIG is fixed to 1.

resolution, and the travel paths used at 0.5, 2.0 and 5.0 Hz are shown in Figure 10. For brevity, the results for the other frequencies, which show similar patterns, are not shown here. The spatial resolution in grid cells with high path coverage is in the range 100-200 km, while it is 200-300 km in the cells with sparse path coverage. This indicates that lateral inhomogeneities with dimension of about 200 km were resolved in the inversion. Areas without or with little path coverage are fixed to the a priori value by the **H** 

matrix in the inversion. The effect of the smoothing matrix  $\mathbf{F}$  is seen at the boundary between well constrained and unconstrained grid cells.

[29] An additional estimation of the model resolution was obtained through a checkerboard test. In this test a synthetic checkerboard model was used with positive variation from the a priori  $Q_{Lg}^{-1}$  value for even grid cells and a negative deviation for odd grid cells. The synthetic data values were computed for the



**Figure 11.** Results from the checkerboard test. The same parameters as in the inversion of the real data were used. (a) Synthetic model with positive and negative deviation from the a priori value and travel paths, which are the same as those used in the inversion of real data at 2 Hz. (b) Result from the inversion of the synthetic data shown in Figure 11a.

same travel paths as used in the inversion of real data (Figure 10). The inversion of the synthetic data was performed with the same damping parameters as used in the inversion of real data. The model vector in the inversion of the synthetic data only included the  $\Delta Q_{Lg}^{-1}$  parameters. The results from this test are shown in Figure 11. It is seen that the smoothness constraint is reflected in the inverted result, however, the checkerboard pattern is clearly resolved in areas with high path coverage. *Leveque et al.* [1993] have shown that smaller structures like in the checkerboard test can be well retrieved in the tomographic inversion, while larger structures are poorly retrieved. However, we consider this checkerboard test as a minimum requirement, indicating the reliability of our results.

[30] The main tectonic features or lateral variations that were resolved in the Q tomography inversion include the differences between the Mixteco-Oaxaca and the Guerrero terranes, the Trans-Mexican Volcanic Belt (TMVB), and the coastal plain of the Gulf of Mexico. The boundaries of these regions are shown in Figure 10. Because of low path coverage north of 20°N, no difference from the average value was obtained for this region. The average  $Q_{Lg}^{-1}$  values obtained as a function of frequency for the various regions are shown in Figure 12, and the linear relationships for  $Q_{Lg}^{-1}(f)$  are given in Table 2.

[31] In regions of recent tectonic activity it is reasonable to expect high scattering and hence low Q [Dainty, 1981]. For the Mixteco-Oaxaca terrane, higher  $Q_{Lg}$  values compared with the

Guerrero terrane were obtained. This result is expected, since the Mixteco-Oaxaca complex is composed of old Precambrian rocks, while the Guerrero terrane has undergone more recent collision tectonics. Previous studies for Guerrero [*Castro et al.*, 1990; *Ordaz and Singh*, 1992] are representatives of the Guerrero terrane, and give similar results to ours. The study by *Castro and Munguía* [1993] for Oaxaca gives smaller Q values for the area 97.2° to 96.3°W and 15.5° to 16.2°N. Low Q values for this region may not be representative for the entire Mixteco-Oaxaca terrane. In our study the resolution in these regions is the highest, which gives us confidence in our results.

[32] Low  $Q_{Lg}$  values, corresponding to high attenuation, were obtained in the TMVB close to the Popocatépetl volcano. Figure 12 shows that the difference in  $Q_{Lg}$  compared with adjacent regions is more pronounced at higher frequencies. This result is similar to that reported by *Shapiro et al.* [2000]. The strong attenuation at higher frequencies in the volcanic zone is probably caused by heating or partial melting of the crustal material and/or by the enhanced scattering caused by the higher level of small-scale heterogeneities due to the active tectonic processes in the volcanic zone. In the remaining part of the TMVB the spatial resolution was low, but there was indication for low  $Q_{Lg}$  values (Figure 10).

[33] Another region where low  $Q_{Lg}$  values were observed is the Gulf of Mexico coastal plain. This is in accordance with the analysis of the efficiency of Lg propagation. The difference in  $Q_{Lg}$  relative to the adjacent regions is more pronounced at low frequencies and disappears above 5 Hz. The fact that the lower  $Q_{Lg}$  is observed at low frequencies suggests that the Lg attenuation in this region is caused by some structural effect. One possible cause could be the variation in the Moho topography [e.g., *Kennett*, 1986; *Campillo*, 1987; *Campillo et al.*, 1993]. Gravity-based studies [*Wollard et al.*, 1956] show that in the Gulf coastal plain the crust is thinner than in central southern Mexico. However, the numerical simulation of Lg propagation in heterogeneous models shows that the variations in Moho topography alone cannot explain the very strong Lg attenuation [e.g., *Maupin*, 1989; *Regan and Harkrider*, 1989; *Cao and Muirhead*, 1993]. Another mechanism



**Figure 12.** Values of  $Q_{Lg}^{-1}$  as a function of frequency for the regions shown in Figure 10.

**Table 2.**  $Q_{Lg}^{-1}(f)$  for Various Regions Obtained in This Study<sup>a</sup>

Region	а	b
Average	$0.00493 \pm 0.00063$	$-0.854 \pm 0.089$
Guerrero	$0.00517 \pm 0.00086$	$-0.872 \pm 0.113$
Mixteco-Oaxaca	$0.00439 \pm 0.00049$	$-0.895 \pm 0.077$
ГMVB	$0.00442 \pm 0.00042$	$-0.486 \pm 0.067$
Gulf of Mexico	$0.00587 \pm 0.00110$	$-0.921 \pm 0.124$
<sup>a</sup> The relationship is	given by $O^{-1}(f) = af^b$	

<sup>a</sup> The relationship is given by  $Q_{Lg}^{-1}(f) = af^{\nu}$ .

for the strong Lg attenuation is the entrapment of the seismic energy in shallow sedimentary layers [e.g., *Knopoff et al.*, 1979; *Zhang and Lay*, 1995; *Shapiro et al.*, 1996]. This mechanism is more likely to be responsible for the low  $Q_{Lg}$  in the Gulf coastal plain.

[34] The study by *Cárdenas et al.* [1998] reported lower Q values for travel paths along the coast as compared with travel paths perpendicular to the coast. This observation seems to agree with the tomography results. In *Cárdenas et al.*'s [1998] study the travel paths along the coast were between 99.5°W and 102°W, and the inland travel paths were from the endpoints toward Mexico City. It is seen that both inland going travel paths propagate in grid cells of higher Q values as compared with the travel path along the coast. Thus their result is explained by local lateral variation of Q. The difference in  $Q_{Lg}^{-1}$  was not seen in section 5.1 because it was determined for the entire coastal region.

[35] These results suggest that significant differences in  $Q_{Lg}$  are preserved between tectonic units, despite these units being subjected to the ongoing subduction process. It is assumed that in the frequency range below 8 Hz, scattering attenuation is more dominant than anelastic attenuation [*Dainty*, 1981; *Mayeda et al.*, 1992]. It is possible that attenuation in the crust is affected by the subduction process through changes in the thermal regime of the upper plate and the release of fluids from the subducted oceanic crust. It seems, however, that these processes are secondary, and  $Q_{Lg}$  mainly reflects scattering attenuation.

## 6. Conclusions

[36] Our study of Lg waves in southern Mexico leads to the following conclusions:

- 1. *Lg* wave propagation is inefficient in the coastal plains of the Gulf of Mexico and in the Gulf of Tehuantepec.
- 2. An average  $Q_{Lg}$  for efficient travel paths in the frequency range 1.6–8 Hz can be expressed as  $Q_{Lg}(f) = 204 f^{0.85}$ .
- 3.  $Q_{Lg}^{-1}$  determined from a single wave type shows a peak value at around 1 Hz.
- 4.  $Q_{Lg}$  for Oaxaca is higher compared with Guerrero, in contradiction to some previous studies.
- 5.  $Q_{Lg}$  is low below Popocatépetl, an active volcano.
- 6. The coastal plain of the Gulf of Mexico is characterized by low  $Q_{Lg}$ .

[37] The results on Lg wave propagation show strong correlation with the crustal structure. Inefficient Lg wave propagation in the coastal plains of the Gulf of Mexico and the Gulf of Tehuantepec is an expected result owing to the presence of thick sediments in these regions. Higher  $Q_{Lg}$  in Oaxaca as compared with Guerrero is explained by the presence of Precambrian, cratonic rocks in the former terrane and prevalence of collision tectonics in the latter terrane. Low  $Q_{Lg}$  below the active Popocatépetl volcano is a consequence of partially molten magma and increased scattering.

[38] Table 2 summarizes  $Q_{Lg}^{-1}$  for different regions and gives an average value for the regions with efficient Lg propagation. This table may be useful in estimation of ground motions from future earthquakes, a task of great importance in Mexico. In



Figure A1. Site terms as obtained in the average  $Q_{Lg}^{-1}$  inversion from horizontal components.

some parts of Mexico the spatial resolution was too low to resolve Q. To improve the regional coverage, additional stations are needed, especially for the regions north of 20°N and east of 92°W.

# Appendix A

[39] Equations (3) and (9) suggest that there might be a tradeoff among site terms, source terms, and  $Q_{Lg}^{-1}$ . To investigate whether this tradeoff is severe, we examined the site terms at each station and the source terms of each event. For this purpose, we used results obtained from the inversion of horizontal components. Figure A1 shows the site terms for selected stations.

[40] The results obtained for the sites CUIG and PPIG, which are located near each other in the Mexican volcanic belt, show large amplification. This result agrees with *Singh et al.* [1995], who reported a maximum amplification of 10 at frequencies between 0.2 and 0.4 Hz for CUIG. For TUIG, high amplification is obtained at high frequencies, which is expected since the station is located on sediments. Little is known about the amplification at the other sites, but the values seem reasonable in view of the local surface geology of the sites.

[41] From the source term, S(f), obtained from the inversion of the horizontal components, we computed the seismic moment,  $M_0$ ,



**Figure A2.**  $M_W$  versus  $M_{\text{SSN}}$ .  $M_W$  is computed from the source term obtained from the inversion using horizontal components.  $M_{\text{SSN}}$  is the magnitude reported by the National Seismological Service (SSN).

assuming a point source dislocation:

$$M_0 = 4\pi\rho\beta^3 S(f \to 0) / (R_{\vartheta\phi}FP) \tag{A1}$$

where  $\rho$  is the density,  $\beta$  is the shear wave velocity,  $R_{\vartheta\varphi}$  is the average radiation pattern (0.55 [*Boore and Boatwright*, 1984]), *F* is the free surface amplification (2.0), and *P* accounts for equal partitioning of energy in the two horizontal components (( $1/\sqrt{2}$ )). The moment magnitude was computed by [*Kanamori*, 1977]:

$$M_W = 2/3\log(M_0) - 6.06, \qquad (A2)$$

where  $M_0$  is in newton meters. Figure A2 compares  $M_W$  obtained from the source term and the magnitude  $M_{\rm SSN}$ , reported by the SSN, which is based on the amplitude of long-period (15 to 30 s) waves [*Singh and Pacheco*, 1994]. From Figure A2 we note that (1)  $M_W$  is, generally, less than  $M_{\rm SSN}$ , and (2) the difference increases for larger earthquakes. Both points 1 and 2 can be explained by the fact that  $M_W$  has been estimated at a period of 5 s, while  $M_{\rm SSN}$  is based on much longer-period waves.

[42] From Figures A1 and A2 we conclude that site and source terms, retrieved from the inversion, are reasonable, and no serious tradeoff has occurred between them and  $Q_{Lg}^{-1}$ .

[43] Acknowledgments. Discussions with Bob Herrmann and Michel Campillo are highly appreciated. We are also grateful to Anatoliy Levshin and Mikhail Barmin for their help with the tomography inversion. The review comments by Steve Myers and two anonymous reviewers have been valuable for improvement of the manuscript and are appreciated. This study was carried out while L. O. was at UNAM on a travel grant provided by the Faculty of Natural Sciences and the Institute of Solid Earth Physics, University of Bergen. This research was partially supported by CONACYT (Mexico) projects J32308-T, 27623-T, and G25842-T and DGAPA (UNAM) projects IN109598 and IN105199.

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