Upper mantle velocity-temperature conversion and composition determined from seismic refraction and heat flow

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[1] We compile upper mantle $P_n$ velocities from seismic refraction/wide-angle reflection surveys in the southern Superior Province of the Canadian Shield and compare them with temperatures at the Moho deduced from heat flow data. Calculated Moho temperatures and $P_n$ velocities correlate well, showing that in this area, $P_n$ depends primarily on temperature. The obtained values of $\partial V(P_n)/\partial T$ depend weakly on the assumed value of Moho heat flow and are on the order of $-6.0 \times 10^{-4} \pm 10\% \text{ km s}^{-1} \text{ K}^{-1}$, within the range of temperature derivatives obtained in laboratory studies of ultramafic rocks. Comparison between observed $P_n$ velocities and predicted values for several mineralogical models at Moho temperatures allows constraints on both the Moho heat flow and the shallow mantle composition. For all Moho heat flows, undepleted (clinopyroxene-rich) mantle compositions do not allow a good fit to the data. For depleted mantle compositions, temperatures consistent with the observed $P_n$ velocities correspond to values of Moho heat flow larger than 12 mW m$^{-2}$. For our preferred Moho heat flow of 15 mW m$^{-2}$, the best fit mantle composition is slightly less depleted than models for average Archean subcontinental lithospheric mantle. This may be due to rejuvenation by melt-related metasomatism during the Keweenawan rifting event. The similarity in $P_n - T$ conversion factors estimated from this empirical large-scale geophysical study and those from laboratory data provides confidence in the absolute temperature values deduced from heat flow measurements and seismic studies.


1. Introduction

[2] A large part of the high-resolution information about the Earth’s interior is provided by seismology, usually through tomographic inversions of large traveltime data sets. This information is often presented in the form of three-dimensional distributions of seismic wave speeds which may be converted into physical parameters such as temperature and density. Variations of seismic wave speed with temperature and pressure [e.g., Sobolev et al., 1996; Goes et al., 2000] have been measured in the laboratory on individual mantle minerals as well as on a few rock samples. For a local study, therefore, interpretation requires a model of mantle composition inferred from geological observations and geochemical constraints [e.g., McDonough and Rudnick, 1998; Griffin et al., 2003]. Calculating temperature from seismic wave speed is affected by significant uncertainties due to the starting compositional model and to the effects of anelasticity and fluids on physical properties. Therefore it is important, where possible, to calibrate this conversion with direct observations within the Earth. For this goal, we combined two data sets that provide the most direct estimates of seismic wave speeds and temperature in the uppermost mantle beneath the Superior Province of the Canadian Shield. In this study, we compare observed upper mantle compressional wave velocities at Moho depth ($P_n$) with those predicted from laboratory data and temperatures estimated from downward extrapolation of heat flow measurements.

[3] We chose $P_n$ velocities because they are determined locally and are not affected by spatial smoothing inherent to tomographic analyses. $P_n$ velocities are deduced from seismic refraction data and are characteristic of the refracted wave that propagates through the mantle just below the Moho discontinuity. These body waves sample the average wave speed over a few kilometers at the wavefront. Spatial resolution along the seismic line depends on the receiver spacing and on local heterogeneity, and is typically $\sim 100 \text{ km}$ [Musacchio et al., 2004]. In contrast, tomographic studies are based on surface wave or teleseismic data and rely on inversions over a block structure. Resolution in the upper mantle is seldom better than $100 \times 100 \text{ km}$ along the
horizontal and 20 km along the vertical [Shapiro and Ritzwoller, 2004]. Herrin and Taggart [1962] and Herrin [1969] have established the regional character of variations of traveltime anomalies and $P_n$ velocities in the United States. These variations have been linked to temperature anomalies [Horai and Simmons, 1968], density anomalies [Pakiser and Steinhart, 1964; Warren and Healy, 1973], and compositional differences in the uppermost mantle [Chung, 1977]. Pakiser [1963] noted that crustal thickness and $P_n$ velocity were related to one another and used an isostatic balance to derive a relationship between $P_n$ velocity and upper mantle density. He realized, however, that seismic velocity is more sensitive to temperature than composition. Black and Braille [1982] examined the relationship between mean $P_n$ velocity and heat flow for the main physiographic provinces of North America. Using a rough thermal model, they obtained an empirical temperature derivative for $P_n$ velocity in approximate agreement with laboratory measurements. Recently, a slightly modified Black and Braille relationship has been proposed for the northern Canadian Cordillera [Lewis et al., 2003].

Rather than seeking correlations between bulk geophysical variables such as crustal thickness, heat flow and $P_n$ velocities, we are interested in temperature variations in the crust and shallow mantle as well as in the lithospheric mantle composition. Heat flow data allow prediction of temperature and, through a mineralogical model, of $P_n$ velocity. These calculations depend on the amount of radioelements in the crust as well as on the shallow mantle composition. Comparing predicted and observed $P_n$ velocities therefore yields constraints on both variables.

The Canadian multidisciplinary geoscience program LITHOPROBE has made available vast seismic data sets that sample all of the Archean and Proterozoic provinces of the Canadian Shield [Clowes et al., 1999]. A summary of crustal structure at $5^\circ \times 5^\circ$ resolution over the entire Canadian Shield based on LITHOPROBE data was provided by Perry et al. [2002]. At the scale of a whole continent juxtaposing provinces of different ages and geological histories, the relationship between mantle seismic velocity and temperature is likely to be contaminated by differences in mantle composition. One of the regions best sampled by seismic refraction/wide-angle reflection data is the southern part of the Archean Superior Province of the Canadian Shield. Because this region has also been extensively sampled by heat flow measurements, it provides an ideal area to study the relationship between mantle seismic velocity and temperature. We have thus compiled all available $P_n$ velocity data and determined upper mantle temperatures from heat flow data in the Superior Province. Because of the dense sampling in this region, the data were interpolated on a $2^\circ \times 2^\circ$ grid. On this scale, we show correlations between $P_n$ and upper mantle temperature for 25 cells where both heat flow and seismic refraction data exist. The velocity-temperature conversion inferred from this large-scale geophysical study is in close agreement with laboratory measurements. We shall show that, in the study area, the Moho temperature varies by about 300 K, implying significant changes of seismic $P$ wave velocity (3%). Such temperature variations are due solely to differences in crustal heat production and are systematic on scales as large as 300–500 km, reflecting the geological structure of the province.

2. Seismic and Heat Flow Data in the Superior Province

2.1. $P_n$ Velocities

The main geological units of the southern Superior Province are shown in Figure 1. The province is made of several east-west trending belts, alternating between volcano-plutonic belts (Uchi, Wabigoon, Wawa, and Abitibi) and metasedimentary belts (English River and Quetico). A gross trend of decreasing age (3.0–2.6 Ga) from north to south reflects the progressive accretion of these belts onto the craton. The region was subjected to major perturbations at 1.9 Ga, which saw the Kapuskasing Uplift, and at 1.1 Ga when the Keweenawan Rift led to the emplacement of large volumes of basalt. $P_n$ velocities and crustal thickness were taken from the LITH5.0 model [Perry et al., 2002] and a recent study of the western part of the province [Musacchio et al., 2004]. The resolution of the data presented here is...
Crustal thickness is shown in Figure 2. The thickest crust reaches ~55 km in the Mid-Continent Rift (Keweenawan) beneath Lake Superior. The distribution of $P_n$ velocity is shown in Figure 3. A correlation between $P_n$ velocity and crustal thickness is apparent through comparison of Figures 2 and 3. Elastic properties depend on pressure and hence variations of Moho depth imply variations of seismic wave speed at constant temperature. From laboratory experiments, $(\partial V/\partial P)_T \approx 0.15$ km s$^{-1}$ GPa$^{-1}$ [Christensen, 1974; Manghnani et al., 1974]. For an average crustal density of 2800 kg m$^{-3}$, the pressure correction is about 4.2 km s$^{-1}$ km$^{-1}$. In the present context, however, such a correction may be neglected and the correlation between $P_n$ velocity and crustal thickness may be attributed solely to temperature. Interpretation requires heat flow data and an accurate crustal model. For example, the thick crust near the Mid-Continent Rift does not necessarily imply elevated Moho temperatures because the volcanic rocks of the rift have low heat production and surface heat flow is low [Perry et al., 2004].

2.2. Seismic Anisotropy

For the purpose of comparing $P_n$ velocities and upper mantle temperatures, one must sometimes account for anisotropy in the continental upper mantle [Vinnik et al., 1992; Silver, 1996; Debayle and Kennett, 2000]. In the southwestern part of the Superior Province, the fast polarization axis for S waves is directed east-west [Silver and Chan, 1991; Kay et al., 1999]. In many cases, it may be difficult to separate the effects of true seismic anisotropy (i.e., due to preferred orientation of minerals) from those of mantle heterogeneity and complex Moho topography [Silver and Chan, 1991]. Here, however, such separation is allowed by two intersecting seismic lines west of the Nipigon Embayment [Musacchio et al., 2004]. In this area, there is no detectable seismic anisotropy in mantle material just below the Moho, i.e., in the $P_n$ velocity. $P$ wave anisotropy of ~6% is determined in only a shallow 50–75 km thick layer lying in the upper mantle 10–15 km below crust of normal thickness [Musacchio et al., 2004]. This layer is interpreted as remnant oceanic lithosphere and does not affect the local $P_n$ velocity determination.

2.3. Heat Flow and Heat Production

Heat flow and heat production data used in this study come from a recent compilation including new measurements for the Superior Province by Perry et al. [2006], where a description of the methods used may be found. The mean heat flow for the Superior Province is 41.2 ± 7.3 mW m$^{-2}$ based on 64 land heat flow determinations. Errors on individual heat flow determinations are estimated. 

Figure 2. Crustal thickness as given by the LITH5.0 crustal model [Perry et al., 2002] modified to include new western Superior data from Musacchio et al. [2004]. (a) Smoothed to $0.05^\circ \times 0.05^\circ$ and (b) true $2^\circ \times 2^\circ$ resolution. The white dots show the location of the seismic refraction/wide-angle reflection lines. The white lines mark the boundaries between the various subprovinces of the Superior Province that are defined in Figure 1.
to be <2 mW m\(^{-2}\). These heat flow measurements sample the southern part of the Superior Province including the Uchi, English River, Wabigoon, Quetico, Wawa, and Abitibi belts (Figure 4). The study area includes Lake Superior where a marine heat flow survey was made [Hart et al., 1994]. These measurements are not as accurate at those made in deep boreholes on land, however they show a consistent pattern with the land heat flow data.

[10] For given values of the surface heat flow, temperatures in the crust and at the Moho discontinuity depend on the amount and vertical distribution of heat producing elements in the crust. Crustal models with a uniform distribution of radioelements give higher Moho temperatures than models in which radiogenic heat production is concentrated in the upper crust. The distribution of radiogenic heat sources in the crust can be estimated from geological and geophysical evidence in combination with values of heat flow at the surface and at the Moho [Perry et al., 2006]. In this region, strong constraints on crustal structure are provided by a deep crustal section exposed at the Kapuskasing site between the Wawa and Abitibi subprovinces.

3. Moho Temperature
3.1. Distribution of Heat Production

[11] On the scale of the Superior Province, one may assume that the Moho heat flow is constant. Evidence and
arguments which support this have been developed at length by Jaupart et al. [1998] and Mareschal and Jaupart [2004], and we only recapitulate the main points. Variations of Moho heat flow, if they exist, would be due to changes of heat supply at the base of the lithosphere which are smoothed out by horizontal heat diffusion. Through ~250-km-thick Archean lithosphere, wavelengths less than 1000 km are strongly attenuated and all wavelengths shorter than 500 km are eliminated. This is supported by analysis of heat flow and heat production data. Heat flow variations can entirely be accounted for by changes of crustal heat production. Variations in Moho heat flow are less than the uncertainty on the heat flow estimates (2 mW m\(^{-2}\)) and cannot be detected.

[12] Using the systematics of heat flow and heat production distributions together with geological and geophysical constraints on the crustal structure, one may obtain estimates of the Moho heat flow between 11 and 15 mW m\(^{-2}\) throughout the Canadian Shield [Pinet et al., 1991; Jaupart et al., 1998]. In order to further constrain crustal compositional models, Guillou et al. [1994] used seismic refraction, gravity, and heat flow data. They concluded that the mantle heat flow is between 7 and 15 mW m\(^{-2}\). Independent heat flow studies in large areas of low heat flow over depleted crust in the Superior Province lead to estimates between 10 and 15 mW m\(^{-2}\) [Mareschal and Jaupart, 2004]. Studies on mantle xenoliths from Kirkland Lake, in the Superior Province, suggest values of 15–18 mW m\(^{-2}\) [Rudnick and Nyblade, 1999; Michaut and Jaupart, 2004]. These various ranges reflect uncertainties in the data and interpretation methods and do not correspond to the magnitude of lateral variations. Our preferred value for Moho heat flow is 15 mW m\(^{-2}\) because it is consistent with both heat flow and xenolith data.

[13] For given values of heat flow at the surface and at the Moho, one may deduce the total crustal heat production but not the vertical distribution of the radioelements. For the purposes of calculating temperatures at the Moho, variability of heat production on the scale of individual geological units (~10–20 km) is irrelevant and one must consider an average heat production model. In the southern Superior Province, Perry et al. [2006] have studied in detail the distributions of heat flow and heat production. They demonstrated that the crusts of the volcano-plutonic belts (Wawa, Wabigoon, and Uchi) are poorly stratified, such that the vertical average of heat production is very close to the surface average. This is supported by geo-physical, petrological and geological studies, which indicate that enriched granitoids account for a significant fraction of the rock types at all crustal levels. In contrast, the intervening metasedimentary belts (English River and Quetico) are characterized by significantly higher values of heat production at the surface and only slightly higher values of heat flow. In these narrow belts, radioelements are enriched in the upper crust. Crustal structure is more complicated, but well documented, in the Abitibi subprovince. The standard model in this subprovince calls for 3 crustal layers of variable thickness: the greenstone volcanics at the surface, an intermediate layer of tonalitic composition, and a granulitic lower crust [Pinet et al., 1991; Guillou et al., 1994; Mareschal et al., 2000]. The heat production in each of these layers is well constrained as they have been extensively sampled, in particular near the Kapuskasing structure where a nearly complete crustal section is exposed [Ashwal et al., 1987; Shaw et al., 1994]. As a general rule, the shallower the heat sources, the lower the Moho temperature. The main contribution to the surface heat flow comes from the intermediate layer of tonalitic gneisses while the upper and lower crust are depleted in radioelements [Pinet et al., 1991]. The difference in Moho temperature between a homogeneous crust and a three layer crust (with the highest heat production in the intermediate crust) is ~25 K, which may be considered negligible.

[14] We carry out calculations for a uniform vertical distribution of heat production in all areas and evaluate a posteriori the validity of the results. This serves to assess the reliability of the thermal models. As discussed above, it is appropriate to assume that the radioelements are uniformly distributed in many belts of the Superior Province. For a constant crustal thermal conductivity \(k_c = 2.5\) W m\(^{-1}\)K\(^{-1}\), the Moho temperature \(T_m\) may be written as

\[
T_m = \left(\frac{Q_i + Q_m}{2k_c}\right)h_c
\]

where \(Q_i\) and \(Q_m\) are the surface and Moho heat flow, respectively, and \(h_c\) is the crustal thickness. The temperature at the Moho calculated in this way is shown in Figure 5 for an assumed Moho heat flow of 15 mW m\(^{-2}\). This model will be referred to as model A.

3.2. Temperature Dependence of Thermal Conductivity

[15] Within the range of crustal temperatures, thermal conductivity varies significantly, which must be taken into account for accurate temperature estimates. Measurements by Durham et al. [1987] are especially applicable to our study as many of their rock samples came from the Superior Province. They determined thermal diffusivity of a wide range of different types of igneous rocks at temperatures and pressures up to 700 K and 200 MPa, respectively. At these temperature and pressure conditions, lattice conduction (phonon transport) is the dominant mechanism of heat transport. Durham et al. [1987] obtained the following equation as a best fit for all their measurements of thermal diffusivity \(\alpha\) (in mm\(^2\) s\(^{-1}\)):

\[
\alpha = 0.47 + 78T^{-1} - 1.31\lambda_Q + 1540\lambda_QT^{-1}
\]

where \(T\) is absolute temperature and \(\lambda_Q\) is the volume fraction of quartz in the whole rock. For the pressure range of crustal studies, pressure effects can be ignored without introducing significant error. The average conductivity for all the surface samples in the Superior Province is 3 W m\(^{-1}\)K\(^{-1}\) at room temperature. We have taken \(\rho = 2700\) kg m\(^{-3}\) and \(C_p = 1.2\) kJ kg\(^{-1}\) K\(^{-1}\), and determined \(\lambda_Q\) as a function of the surface thermal conductivity \(k_c\). Granulite facies rocks which are representative of lower crust lithology have thermal conductivities between 3.0 and 3.5 W m\(^{-1}\)K\(^{-1}\) at room temperature [Joehl et al., 1998], and therefore the same conductivity equation may be used.
throughout the crust. Our expression for the thermal conductivity is

\[ k(T) = 2.264 - \frac{618.2}{T} + k_o \left( \frac{355.6}{T} - 0.3025 \right) \]  

(3)

where \( k_o = 3.0 \text{ W m}^{-1} \text{ K}^{-1} \). Equation (3) gives an average conductivity value of 2.0 W m\(^{-1}\) K\(^{-1}\) in the lower crust.

Radiative heat transport becomes important for temperatures higher than 700–800 K and results in increasing the effective conductivity [Roy et al., 1981; Clauser and Huenges, 1995]. Laboratory experiments have been carried out on mantle minerals at temperatures above 1000 K [Schatz and Simmons, 1972; Schärmeli, 1979; Roy et al., 1981]. The radiative component of thermal conductivity obeys the following law:

\[ k = cT^3 \]  

(4)

where the coefficient \( c = 0.37 \times 10^{-9} \text{ W m K}^{-4} \) [Schatz and Simmons, 1972; Schärmeli, 1979]. Conductivity is thus taken as the sum of lattice and radiative components.

Our working model for the Superior Province is the homogeneous crustal heat production, with a constant heat production equal to \((Q_c - Q_m)/h_c\). The Moho temperature is obtained by integrating the heat conduction equation:

\[ k(T) \frac{dT}{dz} = Q_r + (Q_m - Q_c) \frac{z}{h_c} \]  

(5)

where \( k(T) \) is given by equations (3) and (4). Accounting for temperature-dependent thermal conductivity increases the Moho temperature by as much as \(\sim 150 \text{ K} \). The results are shown in Figure 6 and will be referred to as model B. The Moho temperatures calculated for different values of Moho heat flow \((0 \leq Q_m \leq 25 \text{ mW m}^{-2})\) range between \(\sim 600 \) and 1200 K, with the highest Moho heat flow producing the highest Moho temperatures. Model B is our preferred model for Moho temperature.

4. Correlation Between Moho Temperature and \(P_n\) Velocity

4.1. An Empirical Temperature Derivative for \(P_n\) Velocity

This study involves many independent input variables. In this case, brute force error analysis based on the addition of individual uncertainties leads to very large error estimates. To circumvent this problem, we proceed in two steps. Temperature calculations rely on values for the surface heat flow, mantle heat flow, thermal conductivity and on the vertical distribution of heat production. For \(2^\circ \times 2^\circ\) cells that contain more than 2 heat flow sites, uncertainties on surface heat flow values are small, typically \(<5\%\), and their impact on the Moho temperature may be neglected. We assume that thermal conductivity does not introduce significant errors because of the excellent laboratory measurements of Durham et al. [1987]. As discussed above, the large geophysical and geochemical data set available in the study area allows strong constraints on the vertical distribution of radioelements and the associated temperature uncertainties are small, \(\sim 25 \text{ K}\). We are thus left with the Moho heat flow as the main potential source of error. From Table 1, varying the Moho heat flow by \(5 \text{ mW m}^{-2}\) leads to a change in Moho temperature of \(\sim 50 \text{ K}\). The key point is that, although its absolute value is not known precisely, the Moho heat flow cannot vary by more than \(\sim 2 \text{ mW m}^{-2}\) across the study area. Two recent studies have elaborated on this in detail and need not be repeated here [Mareschal and Jaupart, 2004; Perry et al., 2006]. We thus take a single value of \(Q_m\) throughout the study area and use it as the control variable for uncertainties on temperature. In a second step developed later, we address the difficulty of working with a small range of \(P_n\) velocities.
**Table 1. Average \( P_n \) Velocity, Crustal Thickness, Surface Heat Flow, and Moho Temperature Calculated From Surface Heat Flow Measurements**

<table>
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<th>Longitude, °W</th>
<th>Latitude, °N</th>
<th>( H_c ), km</th>
<th>( P_n ) Velocity, km s(^{-1} )</th>
<th>( Q_{s} ), mW m(^{-2} )</th>
<th>( Q_{m} = 0 ) mW m(^{-2} )</th>
<th>( Q_{m} = 15 ) mW m(^{-2} )</th>
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<td>5</td>
</tr>
<tr>
<td>76</td>
<td>46</td>
<td>38.5</td>
<td>8.20 ± 0.10</td>
<td>45.1</td>
<td>634</td>
<td>779</td>
<td>880</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>74</td>
<td>46</td>
<td>38.6</td>
<td>8.18 ± 0.05</td>
<td>39.2</td>
<td>581</td>
<td>722</td>
<td>822</td>
<td>2</td>
<td>2</td>
</tr>
</tbody>
</table>

\(^a\)\(H_c\) is the crustal thickness, \(Q_s\) is the surface heat flow, \(T\) is the Moho temperature, \(N_{Q}\) and \(N_{P_n}\) are the number of heat flow measurements and the number of tabulated shot points from the refraction data in each \(2^\circ \times 2^\circ\) cell. See text for explanations of temperature calculation.

\(^b\)Error associated with the determination of surface heat flow is <2 mW m\(^{-2}\).

\(^c\)Error associated with Moho temperature calculations for a given value of the Moho heat flow is ±25 K, due to uncertainties in the vertical distribution of radiogenic heat production. Errors quoted for the average \( P_n \) velocity were determined from the supposed error (±0.1 km s\(^{-1}\)) on each velocity determination and the dispersion of values within each cell.
The fact that observed $P_n$ velocity is better correlated (in absolute value) with calculated Moho temperature than with surface heat flow gives further credence to the thermal model.

The empirical temperature derivative of velocity is insensitive to the value of the Moho heat flow. Excluding solutions for zero $Q_m$, which are not realistic, this derivative is $-6.0 \times 10^{-4} \pm 10\% \text{ km s}^{-1} \text{ K}^{-1}$ for a large range of Moho heat flows ($7 \leq Q_m \leq 25 \text{ mW m}^{-2}$). This result is within the range of values for ultramafic rocks determined in the laboratory (Table 3). The agreement between the empirical velocity derivative deduced from geophysical data and laboratory measurements shows that variations of $P_n$ velocities in the Superior Province are indeed due to temperature. Below, we proceed further and make a direct comparison with $P_n$ velocities calculated for specific upper mantle compositions. This comparison allows constraints on both the composition of the upper mantle beneath the Superior Province and the Moho heat flow.

4.2. Anomalous Data Points

Four data points (corresponding to four cells in Figures 3 and 6) stand out as anomalies in a plot of $P_n$ velocity as a function of Moho temperature (Figure 8). The triangles correspond to two cells in the northwestern part of the study area including the English River metasedimentary subprovince (centered at 50°N, 92°W and 50°N, 94°W). A third anomalous cell (identified by a cross symbol and corresponding to 50°N, 88°W) straddles the northeast extremity of the Nipigon Embayment, where mafic intrusives associated with the Keweenawan Mid-Continent rift are present in the crust. The fourth outlier cell (identified by a star symbol and centered at 50°N, 82°W) corresponds to the Kapuskasing heat flow site. Here, we show why these four data points show up as anomalies with respect to the others. In all cases, the problem comes from inadequate heat flow sampling of the heterogeneous crust.

The two anomalous cells in the northwestern corner of the study area encompass the Uchi and Wabigoon volcano-plutonic belts and the English River metasedimentary belt, which have different crustal structures, as discussed above. It is difficult to propose an average crustal model valid for such a geological assemblage. One key factor is that the metasedimentary belts have an enriched upper crust which is not accounted for by the homogeneous crustal model. With the same values of heat flow at the surface and at the Moho, an enriched upper crust could diminish the Moho temperature by as much as 100 K. Accounting for this would bring the Moho temperature for these two areas close to the trend defined by the other points.

The third anomalous cell is located at the edge of the Nipigon Embayment, where late stage mafic intrusions occurred during the Keweenawan rifting event $\sim$1100 Ma [van Schmus et al., 1982]. The two heat flow values for this cell are obtained through a mafic intrusive sequence and are rather low. The cell includes parts of the English River and Quetico belts which are both associated with high heat flows (48 mW m$^{-2}$ [Perry et al., 2006]). The low heat low values can be explained by the abundance of depleted mafic rocks in the crust [Perry et al., 2005] and is not representative of areas that are unaffected by the Keweenawan event. It is thus likely that the average heat flow for the cell is higher than the two determinations available. With a heat flow of 48 mW m$^{-2}$, as elsewhere in the English River and Quetico belts, the Moho temperature is increased by $\sim$100 K, which would remove the anomaly.

The fourth anomalous cell lies in the Kapuskasing uplift region, where depleted lower crustal assemblages have been brought to the surface along a thrust fault [Percival and Card, 1983; Percival and West, 1994]. The single heat flow determination available for this cell was
Wave Velocity in Upper Mantle Rocks

"P" is the velocities are determined with an accuracy of 25–275 200–800 wave-temperature conversion at Moho depth, K Velocity 

The velocity is much greater than that between surface heat flow measured through such depleted crust and is very low (33 mW m⁻²). As in the previous case, accounting for the other rock types and types of crust present in the cell would increase the heat flow and the Moho temperature. In this case, because of the very low heat flow value, the correction to the Moho temperature is likely to be large.

This discussion shows that anomalies in the general trend of \( P_n \) as a function of Moho temperature can all be accounted for. It further illustrates the necessity of accurate crustal models.

4.3. Error Analysis

\( P_n \) velocities are determined with an accuracy of about ±0.1 km s⁻¹ according to Musacchio et al. [2004]. Errors on crustal thickness are estimated to be between 5 and 10%, but these have no significant impact on \( P_n \) velocities, as shown in our previous discussion of pressure effects on seismic wave speeds. The large instrumental error on \( P_n \) velocities may seem overwhelming because it is almost as large as the total variation over the study area. For the purposes of this study, however, one can get around this problem.

We first note that, if ±0.1 km s⁻¹ were an accurate estimate of the true error on \( P_n \) velocity determinations, it would lead to random variations across the study area. In contrast, the data exhibit remarkable large-scale spatial coherence, including cells sampled by independent seismic surveys. One gets better statistics on \( P_n \) velocities by accounting for the number of individual determinations per cell, which may be as large as 13. Table 1 lists errors on the cell-averaged \( P_n \) velocity. Uncertainties were calculated from both the dispersion of individual determinations within a cell and the measurement error, and are small in cells with a large number of data points. One could reduce uncertainties by carrying out a more sophisticated spatial correlation analysis. Another method to reduce the uncertainties would be to impose the experimental value of the temperature derivative of wave speed, which is well-known for given mineral assemblages. One could thus use the empirical (\( P_n, T \)) array to calculate a best fit anchor point with a small uncertainty.

For this study, such refinements are not necessary. On one hand, we are dealing with a rather restricted range of rock compositions for which the temperature derivative of seismic velocity varies little, as will be shown below. On the other hand, the slope of the empirical (\( P_n, T \)) arrays (the temperature derivative of wave speed) is not sensitive to the single control variable (the Moho heat flow) and takes values that are close to laboratory results. Thus, in effect, we seek to compare two parallel arrays, one deduced from laboratory data and the other derived from geophysical measurements, and one needs only to focus on their respective anchor points and the associated control variables: the compositional model and the Moho heat flow.

5. Comparison With a Mineralogical Model for the Upper Mantle

5.1. Calculation of \( P \) Wave Velocity

Calculating the \( P \) wave velocity of a mantle mineral assemblage for in situ conditions requires several inputs: the mantle composition, the thermoelastic properties of individual mantle minerals and a correction for anharmonic and anelastic effects [Shapiro and Ritzwoller, 2004]. Both \( P \) and \( S \) wave velocity-temperature curves have two distinct, almost linear parts: the anharmonic domain (temperatures

<table>
<thead>
<tr>
<th>Regression Variables</th>
<th>( N )</th>
<th>( Q_m, \text{mW m}^{-2} )</th>
<th>( dV/(P_n)\text{d}T \times 10^{-4} \text{km s}^{-1}\text{K}^{-1} )</th>
<th>( \gamma )</th>
<th>( r )</th>
<th>( \alpha )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( T_n - P_n )</td>
<td>25</td>
<td>0</td>
<td>7.0</td>
<td>8.6</td>
<td>0.685</td>
<td>0.2E-3</td>
</tr>
<tr>
<td>( T_m - P_n )</td>
<td>25</td>
<td>7</td>
<td>6.5</td>
<td>8.6</td>
<td>0.707</td>
<td>0.1E-3</td>
</tr>
<tr>
<td>( T_m - P_m )</td>
<td>25</td>
<td>12</td>
<td>6.2</td>
<td>8.6</td>
<td>0.719</td>
<td>0.1E-3</td>
</tr>
<tr>
<td>( T_n - P_m )</td>
<td>25</td>
<td>15</td>
<td>6.0</td>
<td>8.7</td>
<td>0.726</td>
<td>0.00</td>
</tr>
<tr>
<td>( Q_e - P_n )</td>
<td>64</td>
<td>25</td>
<td>5.4</td>
<td>8.7</td>
<td>0.743</td>
<td>0.00</td>
</tr>
</tbody>
</table>

\( ^a \) is the number of data, \( Q_m \) is the imposed Moho heat flow, \( dV/(P_n)\text{d}T \text{ is the } P \text{ wave-temperature conversion at the Moho depth, } \gamma \text{ is the y intercept of the linear regression, } r \text{ is the correlation coefficient, and } \alpha \text{ is the level of significance or the probability of getting a correlation as large as the observed value by random chance when the true correlation is zero. The correlation between Moho temperature } T_n \text{ and } P_n \text{ velocity is much greater than that between surface heat flow } Q_e \text{ and } P_n \text{ velocity. See text for explanations of temperature calculation. The results are plotted in Figures 7 and 8. Read 0.2E-3 as 0.2 \times 10^{-3}.}

Table 2: Correlation Between Moho Temperature, Surface Heat Flow, and \( P_n \) Velocity

Table 3: Temperature Derivatives of \( P \) Wave Velocity in Upper Mantle Rocks

Table 3. Temperature Derivatives of \( P \) Wave Velocity in Upper Mantle Rocks

<table>
<thead>
<tr>
<th>Sample</th>
<th>( -dV/W\text{d}T \times 10^{-4} \text{ km s}^{-1} \text{ K}^{-1} )</th>
<th>( T, \degree \text{C} )</th>
<th>( P, \text{MPa} )</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Peridotite, Ivrea Zone, Italy</td>
<td>4.4</td>
<td>400–700</td>
<td>410</td>
<td>Fieltz [1976]</td>
</tr>
<tr>
<td>Lherzolite xenoliths, Sierra Nevada</td>
<td>6.2–6.9\textsuperscript{a}</td>
<td>25–260</td>
<td>300–900</td>
<td>Peselnik et al. [1977]</td>
</tr>
<tr>
<td>Harzburgite, Antalya ophiolite, Turkey</td>
<td>5.6–6.7\textsuperscript{b}</td>
<td>25–275</td>
<td>200–800</td>
<td>Peselnik and Nicolas [1978]</td>
</tr>
<tr>
<td>Lherzolite xenoliths, Hawaii</td>
<td>6.7–7.1\textsuperscript{a}</td>
<td>25–275</td>
<td>200–800</td>
<td>Peselnik and Nicolas [1978]</td>
</tr>
</tbody>
</table>

\( ^a \) and \( P \) stand for the temperatures and pressures achieved.  
\( ^b \) Mean value for measurements in 3 orthogonal directions.  
\( ^c \) Range for two different samples with different olivine fabrics.  
\( ^d \) Range for measurements in three orthogonal orientations.
<1000°C) and the anelastic domain for temperatures >1000°C, with a narrow transition zone between the two [Shapiro and Ritzwoller, 2004]. Anelastic effects are only important at temperatures exceeding 1000°C [e.g., Karato, 1993] and hence are neglected because Moho temperatures are less than this threshold value. We have not allowed for the presence of free melt and/or water phases in the mantle, which reduce mantle seismic velocities through enhanced anelasticity [Karato and Jung, 1998]. We note that the calculated Moho temperatures are too low for mantle melting to occur. Griffin et al. [2004] found evidence for many episodes of fluid introduction (metasomatism) in the North American continental lithosphere. Such rehydration binds the fluid components within mineral phases which should have less effect on seismic velocity than free fluids.

To investigate errors in P wave velocity calculations due to uncertainties in elastic parameters, we used a recent compilation of laboratory data of seismic velocity and velocity derivatives [Goes et al., 2000]. These errors have been explored for a particular set of upper mantle models [McDonough and Rudnick, 1998] and are illustrated in Figure 9. First, we found that uncertainties in the derivatives of the shear modulus $\partial \mu / \partial T$ and the bulk modulus $\partial K / \partial T$ for olivine have the greatest effect on the calculated velocities. We shall vary these derivatives within the range of experimental data reported by Goes et al. [2000].

Variations of seismic velocity due to changes of the bulk mantle mineralogical composition are significant. Matching observed and calculated $P_n$ velocities therefore yields constraints on the bulk upper mantle composition. Differences in chemical composition of the upper mantle amongst geological provinces or between entire continents have been established by McDonough and Rudnick [1998] and Griffin et al. [2003]. Seismic-geodynamic inversions have placed constraints on the degree of iron depletion in the upper mantle [e.g., Forte and Perry, 2000; Perry et al., 2003; Godey et al., 2004; van Gerven et al., 2004] and yielded values of Mg # in good agreement with xenolith studies at depths of 150–200 km.

The composition of subcontinental lithospheric mantle varies significantly with both depth and location [Griffin et al., 2003, 2004], but there seems to be a systematic difference between Archean samples and younger ones. Table 4 lists two sets of compositional models that are widely used. McDonough and Rudnick [1998] have compiled data from kimberlites and alkali basalt

![Figure 9](image-url)

**Table 4.** Mineralogical Composition of Continental Lithospheric Mantle

<table>
<thead>
<tr>
<th></th>
<th>OL, %</th>
<th>Opx, %</th>
<th>Cpx, %</th>
<th>Gt, %</th>
<th>Mg #</th>
</tr>
</thead>
<tbody>
<tr>
<td>On-craton</td>
<td>83</td>
<td>15</td>
<td>2</td>
<td>91.4</td>
<td></td>
</tr>
<tr>
<td>Off-craton</td>
<td>68</td>
<td>18</td>
<td>11</td>
<td>89.8</td>
<td></td>
</tr>
<tr>
<td>Archon</td>
<td>69</td>
<td>25</td>
<td>2</td>
<td>92.7</td>
<td></td>
</tr>
<tr>
<td>Proton</td>
<td>70</td>
<td>17</td>
<td>6</td>
<td>90.6</td>
<td></td>
</tr>
</tbody>
</table>

*Ol, olivine; Opx, orthopyroxene; Cpx, clinopyroxene; Gt, garnet.*
intrusives to derive an average model for Archean lithospheric mantle which they called “on-craton.” They further obtained an “off-craton” model for Proterozoic and younger continental regions from analyses of massif peridotites, which may be found at Earth’s surface in many Phanerozoic fold belts. Griffin et al. [2003] noted that xenolith data are heavily biased toward southern African kimberlites and added a large data set of xenocrysts carried by alkali basalts. They derived average compositions of Archean and Proterozoic samples, corresponding to “Archons” and “Protons” respectively. The two different sets of models share many characteristics such as clinopyroxene depletion in the Archean and modal contents for off-craton and Proton samples. As shown by Figure 10, the relationship between $V_p$ and temperature for the off-craton model falls far from those of the other three models. We do not expect that this model is appropriate for our study area but will use it to demonstrate that the data can indeed rule it out. Surprisingly, the on-craton and Archon models yield ($V_p$, $T$) curves that are almost identical despite their large modal differences and their different values of Mg #. The Proton model is shifted from the two Archean models in the direction of the off-craton model (Figure 10). Note that the temperature derivatives are slightly different for the two types of mantle composition. Compositional differences have the strongest effect at low temperature and affect $P$ wave velocity more than $S$ wave velocity.

### 5.2. Results

We compare our $V_p - T$ relationship with those of the calculated mineralogical models using the methods of Goes et al. [2000] and Shapiro and Ritzwoller [2004] (Figure 11). There is good agreement between observations and predictions for Archean and Proterozoic models of the lithospheric upper mantle. Within the error limits of

![Figure 10](image1.png)

**Figure 10.** Relationship between $P$ wave velocity and temperature following the method of Shapiro and Ritzwoller [2004]. Mineralogical compositions are based on the work by McDonough and Rudnick [1998] and Griffin et al. [2003] (see Table 4). The difference in $P$ wave velocity between on-craton and off-craton models is 2%.

![Figure 11](image2.png)

**Figure 11.** Relationship between $P$ wave velocity and temperature at the Moho for (a) various models of craton composition and (b) the off-craton composition. The sum of the errors associated with the upper mantle composition and the elastic derivatives is shown by the gray shaded zones and amounts to about ±1%. Crosses, triangles, and circles are ($P_n$, $T$) pairs from seismic refraction and heat flow data for heat flows of 0, 15, and 25 mW m$^{-2}$, respectively. The $P_n$ velocity-temperature values for a Moho heat flow of 15 mW m$^{-2}$ (the preferred solution) are clearly consistent with calculated velocities for an Archean upper mantle mineralogy.
Figure 12. Relationship between $P$ wave velocity and temperature at the Moho. Triangles are $(P_m, T)$ pairs from seismic refraction and Moho temperature calculated for a Moho heat flow of 15 mW m$^{-2}$. The dark gray shaded line is the best fit linear relationship for this large-scale geophysical data set. The sum of the errors associated with upper mantle composition and elastic derivatives is represented by the shaded gray zone. The dotted line is the $P$ wave velocity-temperature correlation for the compositional model of McDonough and Rudnick [1998], and the dashed line is the correlation for their compositional model with increased elastic derivatives. The solid and dash-dotted lines correspond to the compositional model of Griffin et al. [2003] for Archons and Protons, respectively, with increased elastic derivatives.

these mineralogical models, mantle heat flow must be at least 12 mW m$^{-2}$, which is consistent with the independent constraints discussed above. Neither the surface heat flow and heat production data, nor the xenoliths from the Superior Province can justify Moho heat values greater than 18 mW m$^{-2}$ [Perry et al., 2006]. The velocity-temperature relationship for $12 \leq Q_m \leq 18$ mW m$^{-2}$ is consistent with the mineralogical models. The agreement between the observed and predicted curves is improved by using the largest values of $\partial v/\partial T$ and $\partial K/\partial T$ that are compatible with laboratory data. The off-craton model does not allow a satisfactory fit to the data, as expected, mostly because the implied temperature derivative is too high. This shows the sensitivity of the data to the upper mantle composition.

We may proceed further by tightening the range of Moho heat flow values, bearing in mind that none of the xenolith or xenocryst data provide information on depths shallower than about 80 km. Figure 12 and Table 4 show our preferred thermal model, where $Q_m = 15$ mW m$^{-2}$. Given the uncertainties in both $P_n$ velocities and Moho temperature, the data are in good agreement with predictions for Archean and Proterozoic craton compositions. The data are closer to the Proton curve (Figure 12), which seems to be in contradiction with the Archean age of the Superior Province. We must remember, however, that this craton was subjected to two perturbations during the Proterozoic, which have led to the emplacement of numerous dykes near the Kapuskasing uplift and the Keweenawan rift. The Kyle Lake and Attawapiskat kimberlites, to the north of the study area, have yielded samples of the shallow lithospheric mantle (~95 km depth) that are fertile lherzolites [Griffin et al., 2004]. Such compositions do not match the “Archon” model. Garnet minerals from the Sextant Rapids melilitite, within the Kapuskasing Structural Zone, also correspond to fertile lherzolite compositions [Griffin et al., 2004]. These data indicate that the Archean lithospheric mantle beneath the study area has been modified by melt-related metasomatic fluids. Such modification acts to shift the upper mantle composition toward Proton values, which is consistent with our preferred values of the Moho heat flow. The Proton composition consists of a mantle that is less depleted in olivine and has a smaller Mg # (90.6) than the Archon composition (Table 4). Perry et al. [2003] used the tomographic model of Grand et al. [1997] and predicted an average Mg # of ~91 in the region of the Superior Province at 150 km depth, based on cratonic-scale seismic-geodynamic inversions of geophysical observables. However, Mg # was shown to be depth-dependent in the North American lithospheric mantle [Griffin et al., 2004]. Such detailed considerations must be regarded as tentative because of the uncertainties involved, but they illustrate how the combination of heat flow and $P_n$ velocity data can constrain the shallow upper mantle composition which is rarely sampled.

6. Conclusions

$P_n$ velocities from seismic refraction data are well correlated with temperature at the Moho derived from heat flow data. The combination of the two data sets (Moho temperature, $P_n$ velocities) allows a test of the mineralogical composition used in models for tomographic inversions. We calculated temperature and $P_n$ velocity for various mineralogical models of the upper mantle and compared the results to the $(P_n - T_m)$ couples from seismic refraction and heat flow. This comparison demonstrates that the theoretical velocity-temperature conversion used for interpretation of seismic tomographic models is in good agreement with observations. Our preferred solution, which combines constraints on the Moho heat flow as well as on the composition of the lithospheric mantle, has a Moho heat flow of 15 mW m$^{-2}$ and a slightly depleted mantle composition with a Mg # equal to 91.

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